AD-A078 265

NAVAL POSTGRADUATE SCHOOL MONTEREY CA
OPERATIONAL LANCHESTER-TYPE MODEL OF SMALL UNIT LAND COMBAT. (U)
SEP 79 J SMOLER

UNCLASSIFIED

NL



AD A 0 78265

# NAVAL POSTGRADUATE SCHOOL

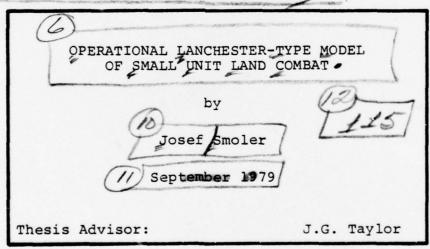
Monterey, California



asterés THESIS,



DOC FILE COPY



Approved for public release; distribution unlimited.

79 12 17 197

JB

#### UNCLASSIFIED

SECURITY CLASSIFICATION OF THIS FAGE (When Date Enter

REPORT DOCUMENTATION F	READ INSTRUCTIONS BEFORE COMPLETING FORM	
1. REPORT NUMBER	2. GOVT ACCESSION NO.	1. RECIPIENT'S CATALOG NUMBER
Operational Lanchester-Type of Small Unit Land Combat	Model	Master's Thesis; September 1979  6. PERFORMING ORG. REPORT NUMBER
Josef Smoler		8. CONTRACT OR GRANT NUMBER(s)
Naval Postgraduate School Monterey, California 93940	/	10. PROGRAM ELEMENT, PROJECT, TASK AREA & WORK UNIT NUMBERS
Naval Postgraduate School Monterey, California 93940		12. REPORT DATE September 1979  13. NUMBER OF PAGES 114
14. MONITORING AGENCY NAME & ADDRESS(II dittorent	tree Controlling Office)	18. SECURITY CLASS. (of this report)  Unclassified  18a. DECLASSIFICATION/DOWNGRADING SCHEDULE
16. DISTRIBUTION STATEMENT (of this Report)		

Approved for public release; distribution unlimited.

- 17. DISTRIBUTION STATEMENT (of the obstract entered in Black 20, if different from Report)
- 18. SUPPLEMENTARY NOTES
- 15. KEY WORDS (Continue on reverse side if necessary and identify by block number)

Lanchester-type Model

20. ABSTRACT (Continue on reverse side if necessary and identify by block number)

A This thesis describes an operational Lanchester-type model of small-unit land combat. It is a time sequenced, deterministic, battalion-level, force-on-force model implemented on a digital computer. In comparison with other existing battalion level

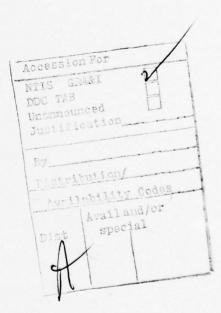
DD 1 JAN 73 1473 EDITION OF 1 NOV 65 IS OBSOLETE S/N 0102-014-6601 |

UNCLASSIFIED
SECURITY CLASSIFICATION OF THIS PAGE (When Date Entered)

SECUMTY CLASSIFICATION OF THIS PAGETWHEN DOIS Entered.

#20 - ABSTRACT - CONTINUED

analytic models, this model contains some new modelling ideas about detection and fire allocation policies.



DD Form 1473 S/N 0102-014-6601

# Approved for public release; distribution unlimited

Operational Lanchester-Type Model of Small Unit Land Combat

by

Josef Smoler
Major, Israel Army
B.S., Technion-Israel Institute of Technology, 1973

Submitted in partial fulfillment of the requirements for the degree of

MASTER OF SCIENCE IN OPERATIONS RESEARCH

from the

NAVAL POSTGRADUATE SCHOOL September 1979

Author	- 1 NO.1
Approved by:	James G. Taylow
	Thesis Advisor
	Verdandsmille
	Second Reader
	Muchael O Averence
	Chairman, Department of Operations Research
	A Shraly
	Dean of Information and Policy Science

# ABSTRACT

This thesis describes an operational Lanchester-type model of small-unit land combat. It is a time sequenced, deterministic, battalion-level, force-on-force model implemented on a digital computer. In comparison with other existing battalion level analytic models, this model contains some new modelling ideas about detection and fire allocation policies.

# TABLE OF CONTENTS

I.	INT	RODU	CTIO	N		7
II.	MOT	IVAT	ION -			10
III.	THE	MODI	EL -			13
	A.	GENI	ERAL	DESCI	RIPTION	13
	в.	MOV	EMEN'	r PROC	CESS FOR ATTACKING UNITS	17
	c.	COM	MAND.	-AND-	CONTROL PROCESS	18
	D.	CHE	CKIN	G LINI	E-OF-SIGHT	18
	E.	DETI	ECTI	ON PRO	OCESS	19
		1.	Тур	es of	Detection	19
		2.	Def	initio	ons	20
		3.			ion of Non-fining Detection ties During (t,t+\Deltat)	20
		4.	Comp	putati e (λ	on of Non-dining Detection	22
		5.	Comp	putat: ities	ion of No Detection Proba- During (t,t+Δt)	26
			a.	Obse	rver Does Not Fire	26
				(1)	Target does not fire during (t,t+Δt)	26
				(2)	Target fires during $(t,t+\Delta t)$	26
			b.	Obset	ever Fires During (t,t+\Deltat)	28
				(1)	Target fires during (t,t+Δt)	28
				(2)	Target does not fire during (t,t+Δt)	29
		6.			bility Effects on Detection	30
		7.	Int	erpre	ation	31

	F.	FIR	E-ALLOCATION PROCESS	31
		1.	Selection of Targets	31
		2.	Priority of Targets	32
		3.	Fire Allocation Procedure	32
	G.	ATT	RITION PROCESS	37
	н.	BAT	TLE-TERMINATION PROCESS	41
IV.	SEN	SITI	VITY ANALYSIS	42
	A.	FIR	E ALLOCATION POLICY	42
	в.	MOV	EMENT DELAY OF A FIRING UNIT (NOD)	44
	c.		ECTION RATE REDUCTION OF A FIRING T (RF)	47
	D.	OBS	ERVATION TIME PROPORTION OF A MOVING T (PM)	47
v.	FUT	URE	ENHANCEMENT AND UTILIZATION	48
	A.	FUT	URE ENHANCEMENT AREAS	48
	в.	UTI	LIZATION	48
APPENI	oix i	A:	PROGRAM LISTING	50
APPENI	DIX I	В:	DEFINITION OF VARIABLES IN COMPUTER PROGRAM	72
APPENI	OIX (	C:	SENSITIVITY-ANALYSIS RESULTS CONCERNING FIRE ALLOCATION	76
LIST (	OF RI	EFER	ENCES	113
INITIZ	AL D	ISTR	IBUTION LIST	114

## I. INTRODUCTION

Although detailed combat models (such as high-resolution Monte Carlo simulations) are heavily used at the tactical level, some analysts and users still have doubts about the use of this kind of model. Detailed combat models (especially high-resolution Monte Carlo simulations) are costly to build, costly to run, require a staff of highly trained personnel to maintain, exercise and modify, are quite demanding in data-base requirements, not easily modified, essentially impossible to use to perform sensitivity and other parametric studies, and are not easily communicated to decision makers.

Though a detailed model is considered by many to be more realistic than an analytic model and to supply more information as output, one can definitely see that there is a price to pay for such detail. This is especially true if one considers some meaningful advantages of analytic models.

Analytic models in contrast are usually much simpler to use and both time and financial resources for their utilization are usually markedly reduced. They are very efficient for conducting sensitivity analysis and their results are readily interpretable, since the dynamics of the combat process are clearly and succinctly described by equations (i.e., they are an efficient tool for communication with decision makers). Analytic models are an

efficient tool for the user too, since they are usually more general thus facilitating their use under more diverse circumstances. Now that we have discussed the pros and cons of the two principal types of small-unit combat models, it remains for us to consider how to decide which one to develop and use under specific circumstances. What should one do to decide which type of model to use? Definitely there is no unique answer to this question. Furthermore, such an answer depends on considerations such as availability of time and money, level of accuracy desired, problem scenario, purposes of model use, etc. Since an analytic model is more abstract than a Monte Carlo simulation, one might ask himself: Do the two types of models describe the same combat process for the same given scenario?

Reference 5 describes a study that was conducted to compare the combat predictions generated by an analytical combat model to those predicted by a more detailed Monte Carlo simulation model. The analytical model was developed against an existing simulation model to determine whether both could generate comparable results. The analytic model was applied to replicate the processes as they were described in the simulation model and not as they might possibly occur in the real world. The conclusions of this study indicate good agreement and suggest that both models essentially describe the same process. In reference 4 it is suggested that the complex model should be used to educate

the analyst while a simple model should be used to communicate with the decision maker. In other words, complex models should be used as research tools to determine basic relations that can be presented to decision makers with simple easily-understood models. In this context the detailed model serves as the "back-up" for the simple model.

## II. MOTIVATION

The BONDER/IUA and its derivatives BLDM and AMSWAG are analytical battalion-level combat models that have been and are currently widely used in the United States for defense planning purposes. After studying documentation for these models, the author decided to build his own smallscale version with certain important changes. For example, the detection and fire-allocation submodels in these models (at least to the extent that they are described in available documentary) have several features that appear to be at variance with both military experience and judgement. Reference 3 describes a sensitivity analysis of BLDM acquisition and firepower allocation models and shows that BLDM is relatively insensitive to changes in non-firing acquisition rates. The analysis explains that this insensitivity is a result of the firepower allocation logic and the fact that firing-cued probabilities in the model have been set to 0.99.

The study in reference 3 recommends that fire-cued acquisition probabilities considerably less than 0.99 should be used in the model and sections of search should be assigned weapon groups. It is also recommended that detection rates for targets lying within a group's primary search sector should be different from those for targets lying outside the sector. The author of this paper also could not strongly

agree with some of the basic assumptions of AMSWAG's detection and fire allocation models. AMSWAG conducts the battle in uniform time steps of 10 seconds each. AMSWAG's detection model keeps track of the comulative acquisition probability that each firer has against each target at any time t and combines this with the new probability of acquisition during the interval  $(t,t+\Delta t)$ . This process is continued as long as line-of-sight is not interrupted. When line-ofsight is interrupted, however, the cumulative probability of acquisition is set to zero and the process will start again if intervisibility again exists at a later point in the battle. According to the author's experience, the cumulative acquisition probability should not be set to zero immediately since the observer still has some idea where to expect the target to appear. The computation of detection probability for each observer against every target must consequently depend on both the observer status (i.e., whether or not the observer fires during the current time interval) and the target status (i.e., whether or not the target fires during the current time interval), whether the target is inside or outside the observer search sector or the observer field of view). This is not done by AMSWAG's detection model.

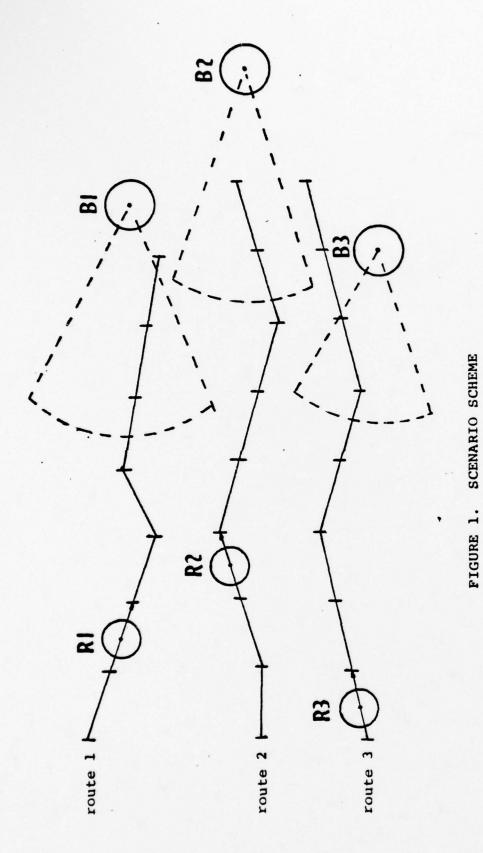
The author of this paper also did not find the AMSWAG's fire allocation model to be a realistic representation of military reality, and consequently has developed a new one based on his previous military experience.

As a result of the discussion above, an analytic battalion level combat model was developed. Although the model was programmed for a specific scenario, it can still be applied to other battalion-level scenarios with relatively few modifications because of its generality.

## III. THE MODEL

### A. GENERAL DESCRIPTION

The model developed in this thesis is a time sequenced, deterministic, battalion-level, force-on-force computer model. The scenario portrays a blue TOW company (3 platoons with 3 TOWS in each) deployed in 3 fixed platoonsized defensive positions (see Bl, B2 and B3 in figure 1). The opponent, a red tank company (3 platoons with 3 tanks in each) conducts an attack along 3 predetermined routes of advance toward the defensive positions. Each route nominally contains a platoon-sized force (see R1, R2 and R3 in figure 1). The model conducts the battle in uniform time steps of 10 seconds each. Figure 2 provides the general scheme for the sequence and flow of events in the model. Basically the sequence of events for each time interval (i.e., 10 seconds) contains five main phases: movement, detection, fire-allocation, attrition and battle-termination (see figure 3). The movement phase is applied to the Red units only. Generally, every Red unit is advanced to the next interval along the associated route unless this unit is destroyed alreay or is in firing status. (In this case the unit will be advanced only every certain number of time intervals.) The detection phase is basically an accumulation process. Detection probabilities during (t,t+Δt) between any two opponent units are computed and combined



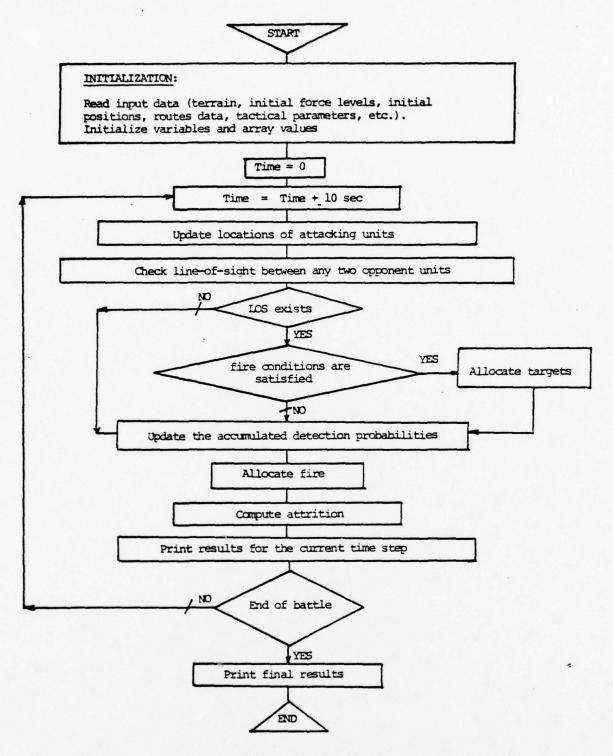


FIGURE 2. FLOW CHART

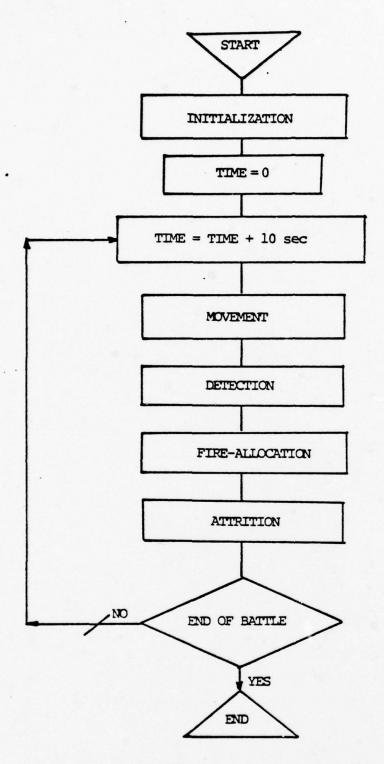


FIGURE 3. GENERAL SCHEME

with the appropriate accumulated probabilities at time t.

Basically the accumulation process can be described by the following equation:

Pr(Unit i does not detect unit j at time  $t+\Delta t$ )

= Pr(Unit i does not detect unit j at time t)
x Pr(Unit i does not detect unit j during t, t+Δt).

The fire allocation phase selects possible targets for every surviving unit, assigns priorities to these targets and determines what fraction of each unit is allocated to fire at each target according to the fire-allocation policy. The attrition phase computes the attrition and the remaining force level for every surviving unit. Since the two forces are homogeneous and use only "aimed-fire", the attrition computation is based on simple Lanchester-type differential equations where the attrition coefficients are computed by the Bonder-Farrel formula. Every such sequence is ended by a battle-termination check process.

## B. MOVEMENT PROCESS FOR ATTACKING UNITS

The 3 attacking tank platoons (see R1, R2 and R3 in figure 1) move along 3 predetermined routes. Each route is divided into intervals, 40 meters length each since a non-firing red platoon is assumed to move one such interval during a time step of 10 seconds (i.e., average speed of 9 mph).

Firing red platoon is delayed NOD times before moving to the next interval. Each interval in each route is represented by its center point coordinates and by its direction. If a red platoon enters to an interval along its associated route then it is considered to be positioned only in the center point of this interval (i.e., maximum location error of ±40 since this is the distance between two consecutive intervals).

#### C. COMMAND AND CONTROL

Command and control are represented in a simple fashion by delaying units which move too fast. If the horizontal distance (along the x-axis) between any two red platoons is more than DISMAX, the leading unit is delayed in order to keep a straight front of the attacking force.

### D. LINE-OF-SIGHT (LOS) DETERMINATION

The existence of line-of-sight between any two opposing units is determined in a subroutine called LOS which was written by Prof. James K. Hartman, Naval Postgraduate School. Each hill in the selected piece of terrain is described by a bivariate normal density function and is characterized by the following parameters:

- 1. Coordinate of the hill center point (xc,yc).
- 2. Peak height
- 3. Standard deviatino corresponds to the x-axis  $(\sigma_{\mathbf{x}})$ .
- 4. Standard deviation corresponds to the y-axis  $(\sigma_y)$ .
- Rotation factor (ρ).

The subroutine is applied by the following FORTRAN statement:

CALL LOS(XA, YA, TMACA, TMICA, SIZEA, XB, YB, TMACB, TMICB, SIZEB, LATOB, LBTOA, VISFRA, VISFRB)

## where:

XA,YA - coordinate of unit A (XA,YA € 0 ÷ 10,000 m)

TMICA - depth below ground surface [meters]

SIZEA - height of the vehicle [meters]

LATOB =  $\begin{cases} 1 & \text{If want LOS with A as observer and B as target} \\ 0 & \text{Else} \end{cases}$ 

LBTOA =  $\begin{cases} 1 & \text{If want LOS with B as observer and A as target} \\ 0 & \text{Else} \end{cases}$ 

VISFRA - fraction of A height as seen by B

VISFRB - fraction of B height as seen by A

0 < VISFRA, VISFRB < 1

#### E. DETECTION

### 1. Types of Detection

A target can be detected in either of two ways:

Random search within a designated section of responsibility

(non-firing detection) or by launch signature given the

target has fired at least one round (firing detection)

[Ref. 1].

# 2. Definitions

Let,

 $P_{ij}(t+\Delta t)$  = the probability that unit j is detected by unit i at time  $t+\Delta t$ 

We assume:

$$P_{ij}(0) = 0 \quad \leftrightarrow i,j$$

- $Q_{ij}(t+\Delta t) = 1 P_{ij}(t+\Delta t) = Probability that unit j is not detected by unit i at time <math>t+\Delta t$
- QV<sub>ij</sub>(t,Δt) = Probability that target j is not visually detected (i.e., non-firing detection) by unit i during [t,t+Δt] provided that j does not fire during this time interval
- QP<sub>ij</sub>(t,Δt) = Probability that target j is not detected by a launch signature during [t,t+Δt] provided that j fires during this time interval
  - 3. Computation of  $QV_{ij}(t,\Delta t)$ Let
- $t_{ij}^{(K)}$  = time for the K<sup>th</sup> firer of unit i to detect one target of unit j. K = 1, 2, ..., S; (t)

where

 $S_{i}(t)$  = number of survivors in unit i at time t.

We assume that  $t_{ij}^{(1)}$ ,  $t_{ij}^{(2)}$ , ...,  $t_{ij}^{(S_i(t))}$  are independent and identically distributed by  $\exp\{\lambda_{ij}\}$  (i.e., exponential distribution with parameter  $\lambda_{ij}$ ), where

 $\lambda_{ij}$  = Non-firing detection rate of one target in unit j by one observer in unit i

 $T_{ij}$  = the time for unit i to detect one target of unit j

Assuming that all  $S_{i}(t)$  survivors of unit i are searching for a target then

$$T_{ij} = \min\{t_{ij}^{(1)}, t_{ij}^{(2)}, ..., t_{ij}^{(s_{i}^{(t)})}\}$$

and  $T_{ij}$  is exponentially distributed with parameter  $S_i^{(t)\lambda}_{ij}$  (i.e.,  $T_{ij} \sim \exp\{S_i^{(t)\lambda}_{ij}\}$ )

 $QV_{ij}$  = Probability that no one of the S<sub>i</sub>(t) survivors of unit j is visually detected by unit i during [t,t+ $\Delta$ t]

= 
$$[Pr(T_{ij} > \Delta t)]^{S_{j}(t)}$$

$$= [e^{-s_{i}(t)\lambda_{ij})\Delta t}]_{j}^{s_{j}(t)}$$

or

$$QV_{ij}(t,\Delta t) = e^{-S_i(t)\lambda_{ij}\Delta tS_j(t)}$$

- 4. Computation of Non-Firing Detection Rate  $(\lambda_{ij})$  Each firer is assigned to a search section (or section of responsibility) which is characterized by two parameters (see figure 3):
  - (a) Section width (ISECWD) where 0  $\leq$  ISECWD  $\leq$   $2\pi$
- (b) Primary direction (IPRDIR) where  $-\pi \leq IPRDIR \leq \pi$  We assume that within the search section the search direction has the following probability density function:

$$f(\theta) = A + B \cos \theta$$
  $-D \le \theta \le D$ 

where,

D = ISECWD/2

 $A = -B \cos D$ 

$$B = \frac{1}{2(\sin D - D \cos D)}$$

 $\theta$  = 0 corresponds to the observer primary direction.

Note: A and B are chosen such that

$$\int_{-D}^{D} f(\theta) d\theta = 1$$

 $f(\theta)$  is called the Limicon Function.

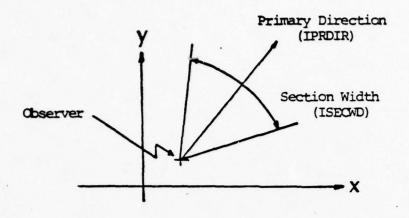


FIGURE 3. SEARCH SECTION

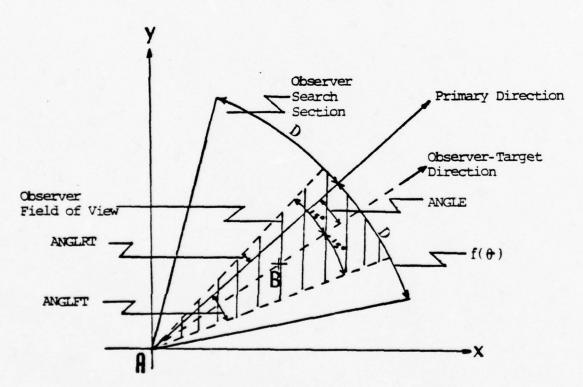


FIGURE 4. OBSERVER-TARGET SCHEME
A = Observer; B = Target

Figure 4 describes the observer-target scheme. Assuming 30° field of view for any observer A target B might be seen only if the observer A is looking at any direction such that ANGRT  $\leq \alpha \leq$  ANGLET where:

ANGLET = 
$$\begin{cases} ANGLE + 15^{\circ} & \text{if } ANGLE + 15^{\circ} \leq D \\ D & \text{if } ANGLE + 15^{\circ} > D \end{cases}$$

ANGLE = the absolute value of the angle between the primary direction (IPRDIR) and the observer-target direction (OTANG)

ANGRT = ANGLE - 15°

Thus,

$$P_k = Pr{ANGRT \le \alpha \le ANGLET} = ANGRT$$
ANGRT

= shaded area in figure 4.

 $\mathbf{P}_{\mathbf{k}}$  is the probability that observer A is looking at direction which enables him to detect target B.

Given that observer A is looking at direction  $\alpha$  such that ANGRT  $\leq \alpha \leq$  ANGLFT, the conditional detection rate  $\{\lambda_{AB} \mid \text{ANGRT} \leq \alpha \leq \text{ANGLFT}\} \text{ is determined by the following regression curve [Ref. 6]:}$ 

$$\{\lambda_{AB} | ANGRT \le \alpha \le ANGLFT\} = 0.003 + [1.453 + TCFACT]$$

$$(0.5978 + 2.188 \times RR^{2} - 0.5038 \times HORVEL]^{-1}$$

where,

TCFACT = Terrain factor

HORVEL = Target horizontal velocity [m/sec]

RR = Equivalent range for a full height target [km]

 $= \frac{R}{PCTVIS} \times \frac{1}{1000}$ 

where,

R = The range between A and B

PCTVIS = Height percentage of visibility of target B (0 < PCTVIS < 1).

The unconditional detection rate (of one observer detecting only one target) is:

$$\lambda_{AB} = \{\lambda_{AB} | ANGRT \leq \alpha \leq ANGLFT\} \times P_{K}$$

 $\lambda_{\mbox{ij}}$  is computed by the subroutine LAMDA using the following FORTRAN statement:

CALL LAMDA (I, J, PCTVIS, DETRAT)

where the variable DETRAT will contain the detection rate of one target in unit j by one observer in unit i.

# 5. Computation of $Q_{ij}(t+\Delta t)$

- a. Observer Does Not Fire During  $(t,t+\Delta t)$ .
  - (1) Target j does not fire during  $(t, t+\Delta t)$ .  $Q_{ij}(t+\Delta t) = Q_{ij}(t) \times QV_{ij}(t, \Delta t)$

where,

$$QV_{ij}(t,\Delta t) = \begin{bmatrix} -s_i(t)\lambda_{ij}^* \Delta t s_j(t) \\ -s_i(t)\lambda_{ij}^* \Delta t s_j(t) \end{bmatrix}$$
$$= \begin{bmatrix} e & & \\ & & \end{bmatrix}$$

where,

$$\lambda_{ij}^{*} = \begin{cases} \lambda_{ij} & \text{if j is a blue unit (stationary)} \\ PM \times \lambda_{ij} & \text{if j is a red unit (moving)} \end{cases}$$

PM = Percent of time that unit i uses for searching targets.  $0.0 \le PM \le 1.0$ 

 $\lambda_{ij}$  is computed by the subroutine LAMDA.

(2) Target j fires during (t,t+∆t)
Let,

 $S_{i}(t)$  = number of survivors in unit i at time t

 $S_{ij}(t)$  = number of survivors in unit j at time t

FR
j = fire rate of each weapon system in unit
j [rounds per second]

FR<sub>j</sub>  $x \Delta t$  = number of rounds fired (at the average) by one firer of unit j during  $(t,t+\Delta t)$ .

$$N = FR_j \times \Delta t \times S_j(t) = Total number of rounds fired by unit j during  $(t, t+\Delta t)$$$

$$= P_K \times 1.0 = P_K$$

Assuming independence, one finds that

assuming independence between the survivors of unit i, we find that

Pr{at least one survivor of unit it = 
$$1 - (1 - P_K)$$
  $(t)$  detects unit j by a fire signature}

$$QP_{ij}(t,\Delta t) = (1 - P_K)^{NS_i(t)} = (1 - P_K)^{FR_j\Delta tS_j(t)S_i(t)}$$

Now,

$$Q_{ij}(t+\Delta t) = Q_{ij}(t)[QV_{ij}(t,\Delta t) + QP_{ij}(t,\Delta t) - QV_{ij}(t,\Delta t)$$

$$\times QP_{ij}(t,\Delta t)]$$

where  $QV_{ij}(t, \Delta t)$  is computed as described in (1).

b. Observer Fires During (t,t+∆t)

We assume that if unit i is busy with firing during  $(t,t+\Delta t)$  then no targets search is considered by unit i during this time interval. Only units within the field of view of unit i can be detected while unit i is firing. In other words, if unit i fires on unit K then OTANG is the direction of the line from the observer i to the target K and only units within OTANG  $\pm 15^{\circ}$  can be detected by unit i (visually or by a fire signature).

- (1) Target j fires during  $(t,t+\Delta t)$  We define the following event:
- A = unit j is within the field of view of unit i with at least one of unit i targets

We assume

Pr{unit i detects unit j by a fire signature during (t,t+Δt) |A} = 1.0

Thus,

Pr{unit i detects unit j by a fire signature during (t,t+ $\Delta$ t)  $|\overline{A}$ }

= 0

Thus,

$$Q_{ij}(t+\Delta t) = \begin{cases} 0 & \text{if event A occurs} \\ \\ g(n) & \text{if j is a Red unit and event } \overline{A} \text{ occurs} \end{cases}$$

$$Q_{ij}(t) & \text{if j is a Blue uni and event } \overline{A} \text{ occurs} \end{cases}$$

where g(n) is an increasing function of n, where n is the number of time intervals elapsed since time t.

(2) Target j does not fire during  $(t,t+\Delta t)$ If event A is the same as defined in (1), then

$$Q_{ij}(t+\Delta t) = \begin{cases} Q_{ij}(t) \times QV_{ij}^{*}(t,\Delta t) & \text{if event $A$ occurs} \\ g(n) & \text{if $j$ is a Red unit and event $\overline{A}$ occurs} \\ Q_{ij}(t) & \text{if $j$ is a Blue unit and event $\overline{A}$ occurs.} \end{cases}$$

where g(n) is the same as defined in (1) and

$$QV_{ij}^{*}(t,\Delta t) = e^{-S_{i}^{*}(t)\lambda_{ij}^{*}\Delta tS_{j}(t)}$$

$$\lambda_{ij}^* = \lambda_{ij} \times RF$$

RF = Reduction factor (the detection rate of unit i
 has to be reduced since this unit fires
 during (t,t+ t) and the search for targets
 is not effective as for a non-firing unit)

$$S_{i}^{*}(t) = S_{i}(t) \times (\sum_{K \in K} PTT_{iK})$$

PTT<sub>iK</sub> = proportion of unit i allocated to unit K

# 6. Intervisibility Effects on Pij (t)

If line-of-sight does not exist between observer i and target j then no accumulation of detection probability takes place during the current time interval (i.e.,  $P_{ij}(t)$  remains the same). If line-of-sight does not exist during more than 3 consecutive time intervals then  $P_{ij}(t)$  is set to zero (i.e.,  $P_{ij}(t) = 0$ ) and the accumulation process will start again from zero if line of sight again exists at a later point in the battle.

The motivation for this decision rule is seen by the observation that even if observer i loses line-of-sight

with target j for a short time, he still probably has some idea where to expect the target to appear again.

This decision rule was chosen somewhat arbitrarily, and some other time decreasing function may be employed if desired by the user.

# 7. Interpretation

P<sub>ij</sub>(t) can be interpreted as the <u>average</u> fraction of unit i that detects unit j. Any detection that occurs during the n<sup>th</sup> time interval is used only in the next (i.e., (n+1)<sup>st</sup>) time interval, since that detection represents new knowledge gained during the entire n<sup>th</sup> interval under the conditions existing in that interval.

#### F. FIRE ALLOCATION

The first step in a firing event is to determine what fraction of each unit is allocated to fire at each target. Each firing unit does not have to select and fire at just one target. Rather, each firing unit might apportion a fraction of itself against several targets.

# 1. Selection of Targets

The following conditions are necessary for it to be possible for unit j to be a target of unit i:

- (a) Line-of-sight must exist between unit i and unit j.
- (b) The range between the two units should be within the interval [RMIN<sub>i</sub>,RMAX<sub>i</sub>] where the two limits are determined by the weapon system type of unit i and by tactical considerations.

(c) 
$$P_{ij}(t-\Delta t) > 0$$
.

# 2. Priority of Targets

Since the two forces are homogenous, the priority of a target is taken to be a function of range only (since (homogeneous type of target is not considered).

# 3. Fire Allocation Procedure

It will be easier to explain this procedure by numerical example. First, for each unit i we find all the targets j which satisfy the three necessary conditions for being targets (see paragraph 1).

Second, we rank all the targets of unit it by the range.

Let

$$s_i(t) = 100$$

$$RMAX_i = 3000 m$$

$$RMIN_i = 500 m$$

and assume we have the following situation:

Target (j)	Range	Priority	P <sub>ij</sub> (t)
3	750	1	0.2
1	820	2	0.9
2	900	3	0.7

If we allocate fire to each target j as if this target is the only one we have:

Target (j)	Max Allocation = $P_{ij}(t) \times S_{i}(t)$
3	$P_{i3}(t) \times S_{i}(t) = .2 \times 100 = 20$
1	$P_{i1}(t) \times S_{i}(t) = .9 \times 100 = 90$
2	$P_{i2}(t) \times S_i(t) = .7 \times 100 = _{70}$

Total: 180

For example, since  $P_{i3}(t) = 0.2$  means that 20% of unit i have detected unit j at time t, then not more than 20% of unit i can fire on unit j. Thus, at the maximum not more than  $P_{i3}(t) \times S_i(t) = 0.2 \times 100 = 20$  firers out of 100 survivors of unit i can be allocated to fire at unit j. We can obviously see that we need 180 survivors in unit i if we want to allocate fire to each target as if this target is the only one. Since  $180 > S_i(t) = 100$  we can't do that. Let us define the following events:

- $D_j$  = Target j has been detected by unit i, j = 1,2,3
- $\overline{D}_{j}$  = Target j has <u>not</u> been detected by unit i, j = 1,2,3

If the fire policy is to allocate 100% of the firepower of unit i to the most prior target then we have:

Situation	Probability	Engaged Target
$\overline{D}_1 \cap \overline{D}_2 \cap \overline{D}_3$	$0.1 \times 0.3 \times 0.8 = 0.024$	-
$D_1 \cap \overline{D}_2 \cap \overline{D}_3$	$0.9 \times 0.3 \times 0.8 = 0.216$	1
$\overline{D}_1 \cap D_2 \cap \overline{D}_3$	$0.1 \times 0.3 \times 0.8 = 0.056$	2
$\overline{D}_1 \cap \overline{D}_2 \cap D_3$	$0.1 \times 0.3 \times 0.2 = 0.006$	3
$D_1 \cap \overline{D}_2 \cap D_3$	$0.9 \times 0.7 \times 0.8 = 0.504$	1
$D_1 \cap \overline{D}_2 \cap D_3$	$0.9 \times 0.3 \times 0.2 = 0.054$	3
$\overline{D}_1 \wedge D_2 \wedge D_3$	$0.1 \times 0.7 \times 0.2 = 0.014$	3
$D_1 \cap D_2 \cap D_3$	$0.9 \times 0.7 \times 0.2 = 0.126$	3

The fire distribution is:

$$Pr{Target 1 will be engaged} = 0.216 + 0.504 = 0.72$$

Pr{Target 2 will be engaged} = 0.056

Pr{Target 3 will be engaged} = 0.20

Thus, if the same battle is repeated many times then in 72% of the times all the  $S_{i}(t) = 100$  survivors of unit i are allocated to target 1, in 5.6% of the times to target 2 and in 20% of the times to target 3.

If the fire policy is as follows:

# of targets	% of unit	i allocat	ed to each target
	ı <sup>st</sup>	2 <sup>nd</sup>	3 <sup>rd</sup>
1	100%		
2	80%	20%	
3	80%	15%	5%

then we have,

Situation	Probability	<u>A11</u>	ocation	
		tgt 1	tgt 2	tgt 3
$\overline{D}_1 \cap \overline{D}_2 \cap \overline{D}_3$	0.024	-	-	-
$D_1 \cap \overline{D}_2 \cap \overline{D}_3$	0.216	100%	-	-
$\overline{D}_1 \cap D_2 \cap \overline{D}_3$	0.056	-	100%	-
$\overline{D}_1 \cap \overline{D}_2 \cap \overline{D}_3$	0.006	-	-	100%
$D_1 \cap D_2 \cap \overline{D}_3$	0.504	808	20%	_
$D_1 \cap \overline{D}_2 \cap D_3$	0.054	20%	-	80%
$\overline{D}_1 \cap \overline{D}_2 \cap \overline{D}_3$	0.014	-	20%	808
$D_1 \cap D_2 \cap D_3$	0.126	15%	5%	80%

E[percent of fire of unit i =  $100 \times 0.216 + 80 \times 0.504 + 20 \times 0.054$ allocated to target 1] +  $15 \times 0.126 = 64.89$  E[percent of fire of unit  $i = 100 \times 0.056 + 20 \times 0.504$ allocated to target 2]  $+ 20 \times 0.014 + 5 \times 0.126$ 

= 16.59

E[percent of fire of unit i =  $100 \times 0.006 + 80 \times 0.054$ allocated to target 3] +  $80 \times 0.014 + 80 \times 0.126$ 

= 16.12

If we compare the two fire policies we have,

		Tgt 1	Tgt 2	Tgt 3	Total
Policy	I	72%	5.6%	20%	97.6%
Policy	II	64.89%	16.59%	16.12%	97.6%

#### Comments:

- (1) The big change of fire allocation to target 2 is explained by the fact that situation 5 (i.e.,  $\overline{D}_1 \cap D_2 \cap \overline{D}_3$ ) has high probability of occurrence (0.504) and 20 firers of unit i are allocated to target 2 in this case.
- (2) In both cases only 97.6 firers of unit i are allocated since there is a positive probability of not detecting all the three targets (i.e., positive probability for  $\overline{D}_1 \cap \overline{D}_2 \cap \overline{D}_3$ ) and in this case no fire is allocated at all.
- (3) This method gets more complicated as the number of targets becomes larger.

#### G. ATTRITION

Since the two forces (i.e., attacker and defender) are taken to use only "aimed" fire, variable coefficient Lanchester-type equations of modern warfare [see Ref. 2] are used to assess force-on-force attrition. For each time interval  $[t,t+\Delta t]$  let,

 $S_{i}(t)$  = number of survivors in unit i at time t

B<sub>i</sub> = the group of Blue units who fire against unit i

A

ij = the rate at which one firer of unit i

kills unit j targets. (Attrition rate

of unit j by one firer of unit i)

PROP = proportion of unit i allocated to fire against unit j.

These parameters are computed for each time interval. The attrition-rate coefficient  $A_{\mbox{i}\,\mbox{j}}$  is computed according to

$$A_{ij} = \frac{1}{E(T_{ij})}$$
,

where  $T_{ij}$  is the time for one firer of unit i to kill one target of unit j under the conditions existing in this time interval.  $E(T_{ij})$  is computed by the Bonder-Farrell formula (see Ref. 7):

$$E(T_{ij}) = t_a + t_1 - t_h + \frac{t_h + t_f}{P(K|H)} + \frac{t_m + t_f}{P(h|m)}$$

$$\times \left\{ \frac{1 - P(h|h)}{P(K|H)} + P(h|h) - p \right\}$$
 (1)

where,

t<sub>a</sub> = time to acquire a target,

t<sub>1</sub> = time to fire first round after target
acquired,

th = time to fire a round following a hit,

t<sub>m</sub> = time to fire a round following a miss,

t<sub>f</sub> = projectile time of flight,

P = Probability of hit on first round,

P(h|h) = Probability of a hit on a round following
 a hit,

P(h|m) = Probability of a hit on a round following a miss,

P(K|H) = Probability of destroying a target given
 it is hit.

This formula (1) holds for the following conditions:

- (1) Markov-dependent fire with parameters P, P(h|h) and P(h|m). (I.e., Hit probability of any round depends only on the result of the previous round.)
- (2) Geometric distribution for the number of hits required for a kill with parameter P(K|H) (i.e., accumulated damage is not considered!).

If the firing weapon system is TOW then we assume P(K|H) = 1.0 and p(h|m) = p(h|h) = p. In this case we have

$$E(T_{ij}) = t_a + t_l + t_f + \frac{(t_m + t_f)(1 - p)}{p}$$

If the firing weapon system is a tank then we assume  $P(K|H) = 1.0 \text{ (because of lack of information) and } t_f \approx 0.$  In this case we have:

$$E(T_{ij}) = t_a + t_1 + \frac{t_m}{p(h|m)} \{1 - p\},$$

The attrition of each Blue unit j is described by the following differential equation:

$$\frac{ds_{j}(t)}{dt} = -\sum_{i \in R_{j}} A_{ij}(S_{i}(t) \times PROP_{ij})$$

and similarly the attrition of each Red unit i is described by:

$$\frac{ds_{i}(t)}{dt} = -\sum_{j \in B_{i}} A_{ji}(s_{j}(t) \times PROP_{ji})$$

where the attrition coefficients  $A_{ij}$  and  $A_{ji}$  are computed by Bonder-Farrell's model.

The basic differential equations of force-on-force attrition are approximated by the following Euler-Cauchy difference equations:

$$S_{i}(t+\Delta t) = Max\{0,S_{i}(t) - \sum A_{ji}(S_{j}(t) \times PROP_{ji})\Delta t\}$$
  
For each Blue unit i

$$S_{j}(t+\Delta t) = Max\{0,S_{j}(t) - \sum_{i \in B_{j}} A_{ij}(S_{i}(t) \times PROP_{ij}\Delta t)\}$$
  
For each Red unit j

### COMMENTS:

- (1) While computing attrition in a given scenario we can consider all the targets as stationary since the defender is in fixed positions and since the hit probability of a TOW against moving target is almost the same as for stationary (given that the target is not too close). Thus also the Red units can be considered as stationary for attrition computation purposes.
- (2) This attrition model does not consider the problem of intervisibility "windows" for the TOW.
- (3) Hit probabilities as P(h|h) and P(h|m) are functions of: size of the target (full target or turret target), type of ammunition (HGAT or APFSDS), Range, angle between the firer and the target etc. Since most of this information is classified only full size targets,

- APFSDS ammunition (for tanks) and the range were considered while running the program in the computer.
- (4) Artillary is not considered in this model. One should remember that artillary reduces very drastically the TOW hit probability (but not too much the tank's hit probability).

## H. BATTLE-TERMINATION PROCESS

The breakpoint for each unit is 100% lost of its initial force level. The battle is terminated when either:

- One of the two opponent forces (i.e., Red or Blue) is annihilated (i.e., its 3 platoons have reached the breakpoint).
- 2. The average distance between the surviving Red force and the surviving Blue force is "too close."

# IV. SENSITIVITY ANALYSIS

Sensitivity study was done without considering the line-of-sight factor (i.e., it was assumed that line-of-sight exists all the time) in order to make the battle more active (i.e., fights are more frequent and more units are involved in every one of them) and thus more sensitive to most of the parameters.

#### A. FIRE ALLOCATION POLICY

Three fire allocation policies were tested:

Policy	l Target	2star	gets 2nd	ıst	3 targe	ets 3rd
1	100%	100%	-	100%	-	-
2	100%	80%	20%	80%	15%	5%
3	100%	50%	50%	33.3%	33.3%	33.3%

Table 1. Fire Allocation Policies

Appendix C describes the output for three battles corresponding to the three different fire allocation policies. Table 2 summarizes the main events in each battle for comparison purposes.

E V		Po	licy 3			P	olicy 2			Po	olicy :	ı
E N T	UD	T	RTL	BTL	UD	T	RTL	BTL	UD	Т	RTL	BTL
1	6	40	0.131	0.333	6	40	0.131	0.333	6	40	0.128	0.333
2	1	140	0.472	0.444	1	150	0.484	0.503	1	150	0.464	0.517
3	2	210	0.710	0.508	4	240	0.623	0.667	4	210	0.557	0.667
4	4	300	0.837	0.667	3	410	0.864	0.712	3	390	0.760	0.714
5	3	440	1.00	0.68	2	440	1.00	0.723	2	440	1.00	0.759

Table 2. Fire Allocation Sensitivity

where,

EVENT occurs when a unit is destroyed

UD = The number of the destroyed unit

T = time (sec)

RTL = Red total lost (percentage)

BTL = Blue total lost (percentage)

## The conclusions drawn from these results are:

- a. Policy 3 should be preferred to the Blue force since its total lost is consistently smaller when it uses this policy.
- b. Policy 1 should be preferred by the Red force for the same reasons.
- c. These conclusions are appropriate only for the given scenario and they might be different for other scenarios.

- d. The differences are relatively small but they might be larger for different scenarios (i.e., different force structure, weapon characteristics, etc.).
- e. In this sensitivity study the <u>same</u> fire allocation policies were tested for both sides. Future work might be done to test different policies for the two forces.

#### B. MOVEMENT DELAY OF A FIRING UNIT

A firing Red unit is delayed NOD time intervals before moving to the next route interval.

A sensitivity study of this parameter was done for NOD = 2, 3, 4, 5, 6, 8. Table 3 describes the results of this study. Table 4 shows the sensitivity of battle termination time to the parameter NOD. One can see that a change from NOD = 2 to NOD = 6 extends the battle time by more than 25%. No change is caused by changing NOD from 6 to 8. Table 5 shows the sensitivity of Blue total lost (fraction of initial strength) to changes in NOD. No significant change is caused to this variable by changing the value of NOD from 2 to 4. A change of 6% is caused by changing NOD from 4 to 5 and 8% by changing NOD from 4 to 6. We can also see that from NOD = 5 and further on the event's sequence is changed although the final results are not significantly changed.

•	TOC	ß.	æ	13	Œ	32	1.0
NOD = 8	H	40	150	240	430	550	RTL = ] BTL = (
	5	9	Н	7	4	က	ě řa
9	100	Œ	80	13	(34)	32	1.0
9 = QQN	H	40	150	240	430	550	RTL = BTL =
	9	9	7	7	4	e	ř ří
2	100	Ē	6	14	<u>[24</u>	32	1.0
NOD = 5	H	40	150	260	330	480	RTL = BTL =
	9	9	٦	7	4	e	RT B
4	IOC	Ē	6	Œ	33	32	1.0
NOD = 4	H	40	150	250	440	460	RTL = BTL =
	e	9	٦	4	3	7	F. F.
3	IOC	Ē4	10	Œ	33	33	1.0
NOD = 3	E	40	150	240	410	440	11 19
	9	9	7	4	3	7	RTL
= 2	IOC	Œ	11	Œ	33	33	.0
NOD = 2	E	40	150	220	380	410	RTL = 1.0 BTL = 0.726
	9	9	7	4	3	7	RTI

TABLE 3. NOD SENSITIVITY ANALYSIS

LOC = LOCATION

T = TIME

TD = TARGET DESTROYEE

RTL = RED TOTAL LOST (fraction of original strength) BTL = BLUE TOTAL LOST (Fraction of original strength)

F = FIXED POSITION

NOD	Battle	Termination	Time	(sec)
2		410		
3		440		
4		460		
5		480		
6		550		
8		550		

Table 4. NOD VS BATTLE TERMINATION TIME

NOD	Blue Total Lost					
2	0.726					
3	0.723					
4	0.724					
5	0.682					
6	0.667					
8	0.667					

Table 5. NOD VS BLUE TOTAL LOST

### C. DETECTION RATE REDUCTION OF A FIRING UNIT

The detection rate of a firing unit is reduced by a multiplicative factor RF  $(0.0 \le RF \le 1.0)$  in comparison to that of a non-firing unit. This is done, since it is hypothesized that the search effectiveness is not the same in both cases. The sensitivity of results to changes in this parameter (RF) was done for RF = 0.2, 0.3, 0.4, 0.5, 0.6, 0.8. It was found that the battle outcomes are not significantly sensitive to changes in the RF parameter.

## D. OBSERVATION TIME PROPORTION OF A MOVING UNIT

The parameter PM is defined as the proportion of time a moving unit spends for targets search. Sensitivity study of this parameter (PM) was done for PM = 0.15, 0.25, 0.35, 0.45, 0.55.

It was found that the battle outcomes are <u>not signifi-</u>
<u>cantly sensitive</u> to changes in the PM parameter.

### V. FUTURE MODEL ENHANCEMENT AND UTILIZATION

#### A. FUTURE ENHANCEMENT AREAS

The following additions or improvements in the model are recommended:

- Addition of artillery to both sides. Artillery has significant suppression effects on the TOWs.
- 2. Addition of information (target acquisition) handoff from one unit to another.
- 3. Addition of ability to play minefield and barriers.
- 4. Addition of the effects of close air support.
- 5. Modification to the interactive mode.

In such a mode tactical decisions (e.g., route selection) could be input by players as the battle evolves. Additionally, some more predetermined alternative routes and alternative fire allocation policies can be programmed. In this case, the players of both sides (company or platoon commanders) can decide after each time interval which tactic of fire allocation to use, which route to choose and to ask for artillery or close air support (with appropriate amount of delay).

## B. UTILIZATION

The model with the additional recommended improvements might be used as a tool for <u>tactical training</u> (battalion, company and platoon leaders) or <u>tactical planning</u> (effect

of different structure of forces or units, types of weapon systems, fire allocation policies, minimum or maximum ranges of fire, etc.) at the battalion level. APPENDIX A

PROGRAM LISTING

CCFMON /GRP1/ IPRDIR(6), ISECWD(6), WVT DIR(6), X(6), Y(6), SPD(6)

COMMON /GRP2/ TA(2), TH(2), TH(2), TH(2), TF(2), TF2(2), TF3(2),

IP (2,6), PHH(2,6), PHM(2,6), PKH(2,6), TF(2)

COMMON /GRP3/ NBU, NRU, FL(6), FD(6), NJ1(3), XIC(3,100), YIC(3,100),

INDIST A (6), IN(6), CRF, DIST (6,6), VISFR, SIZETK,

INDIST A (6), IN(6), SRF, DIST (6,6), VISFR, SIZETK,

INCOSC(6,6), VISFR (6,6), RMINTK, RMINTW, RWXTW, GP, TCMFR, THE

INCOSC(6,6), VISFR (6,6), RMINTK, RMINTW, RWXTW, GP, TCMFR, THE

COMMON /GRP5/ LDT(6), RMINTK, RMINTW, RWXTW, GP, TCMFR, THE

CCMMON /HILLS/ XC(100), YC(100), PEAK(100), SX(100), SY(100), RHO(100), THE

CCMMON /HILLS/ SCALE(100), TWORH G(100), TWOSCL(100), SASE

CCMMON /HILLS/ SCALE(100), TWORH G(100), TWOSCL(100), SASE

CCMMON /HILLS/ CXC(150), CYC(150), CPEAK(150), CPXX(150), CPYY(150)

THE

CCMMON /COVER/ CXC(150), NCVELS

CCMMON /COVER/ CXC(150), NCVELS

CCMMON /COVER/ CXC(150), NCVELS

CCMMON /COVER/ CXC(150), NCVELS

CCMMON /GRID/ LST(10,10), NHL(10,10), LISTC(4C0), KRREP(100), KTREP

THE

CCMMON /GRID/ LST(10,10), NHL(10,10), LISTC(4C0), KRREP(150), THE MP=0
21=0.00001
21=0.00001
Call SETUP
Call SETUP
A SUBROUTINE TO READ THE TERRAIN DATA FOR THE LINE-OF-SIGN.
SUBROUT INE
READ(5,100) NBU, MRU, AVSP, SIZETK, SIZETW, RWINTK, RWINTW,
IDO FORWAT (IZ,1X, IZ,1X,F4.1,1X,F4.2,1X,F6.1,1X, IPRDIR (6), IS ECWD(6), MVT DIR (6), X(6), Y(6), SPD(6)

TA(2), TI(2), TH(2), TM(2), TFI (2), TF2(2), TF3 (2),

), PHM(2,6), PKH(2,6), TF(2)

NBU,NRU,FL(6), FO(6), NJI (3), X IC(3, 100), Y IC (3, 100),

SP 11.1 X, 'NRU=', II, 1X, 'AVSP=', F4.1, 1X, 'SIZETK=', F4.2, 1X, 'RMXTK=', F6.1, 1X, TNKFR', NCD', TOWFR', NCD', TNKFR', NCD', TNKFR', NCD', TNKFR', F6.3, 1X, 'RF=', F6.3, 1X, 'RF=',

00000000

UU

```
(I), X(I), Y(I), IPRDIR(I), ISEC WD(I), MVTDIR(I),
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   ,3,1X
L=hRith NBI

Y=6506, 0

X=500, 0

X=500, 0

X=500, 0

Y=700, 0

Y=100, 0

Y=
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   Y FL(I) = ', F6.3, 1X, 'X(I) = ', F9.

Y MYTDIR(I) = ', I3, IX, 'SPD(I) =
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         MR 1 TE ( 6 L S PD ( 1 ) F C R MAT ( 1 ) F C R
```

```
m -
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              EAD(5) TA(1), TI(1), TH(1), TF1(1), TF2(1), TF3(1)

105 FORMATT (4F5.3, 1x);

READ(5, 515/P(1, J), PHH(1, J), PHM(1, J), PKH(1, J)

85 FORMAT (4F5.3, 1x);

READ(5, 515/P(1, J), PHH(1, J), PHM(1, J), PKH(1, J)

85 CON TIVUE

85 CON TIVUE

86 CON TIVUE

87 FORMAT (4F5.3, 1x);

87 FORMAT (4F5.3, 1x);

87 FORMAT (4F5.3, 1x);

88 FORMAT (1, J) = 0.05

89 FT (2, Z) = 0.05

89 FT (1, Z) = 0.05

89 FT (2, Z) = 0.05

80 FT (2, Z) = 0.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                RED UNITS
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                92
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                6 0T 0
6 0T 0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       GOTO
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             0F
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         1 SMA X= 150. C

0 9 1=1, NRU

F(IUSTAT(I)-E9.2)

F(I)=NF(I)+1

F(NF(I)-LT.NOD) GC

F(I)=0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                LOCATION
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             UFDATE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         SAMPLE SA
                                                                                             105
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   5 18
                                                                                                                                                                                                       515
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              19
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               91
```

```
LOS(XX1,YY1,TMACI, 0.0, SIZETK, XX2, YY2, TMACJ, 0.0, SIZETW,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           AND TAPGETS SELECTION
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           BETWEEN UN ITS
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   11
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   GOTO
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      USTAT (1).E0.2) GOTO 12
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           7 CONTINUE

DC 12 1=1,NRU

NT(1)=0

1F(1USTAT(1).EQ.2) GOTO 12

DG 16 14(1)

XX1=X(1)

YY1=Y(1)

XX2=X(1)

XX2=X(1)

XX2=X(1)

XX2=X(1)

XX2=X(1)

XX2=X(1)

XX1=X(1)

XX1=X(1)

XX1=X(1)

XX1=X(1)

XX2=X(1)

XX2=X(1)

XX2=X(1)

XX2=X(1)

XX2=X(1)

XX2=X(1)

XX1=X(1)

XX2=X(1)

XX2=X(1)

XX2=X(1)

XX2=X(1)

XX2=X(1)

XX2=X(1)

XX2=X(1)

XX1=X(1)

XX2=X(1)

XX2=X(1)
FOUNTINUE

K9=NRU-1

D0 10 1=1 (K9

K8=1+1

D0 11 J=K9

K8=1+1

D0 11 J=K8

K8 = 1 (H0 = 1 (H0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           CHECK
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 13=J

11(13)=11(13)-1

K7=11(13)

X(13)=X1C(13)K7

Y(13)=Y1C(13)K7

MVTDIR(13)=1DIF

1PRDIR(13)=1DIF

60T 0 11

60T 0 11
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           LINE--0F-SIGH
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                17 J=K, L
J)=0
TINUE
12 I=1, NRU
[)=0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        133
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            5 C
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     51
```

| THE | THE

```
11.4 TOB 1.4 BTOA .VISFRA, VISFRB)
VISFRB-1.0
VICSC(1, 1) = 0
VIC
```

S

| AA=1 |

```
IF (PROP. EQ. 0.0) GCTN 34
CALL LAMBA(1.1) GT-0160 TO 36
CALL LAMBA(1.1) FCTVIS, DETRAT, PSUBK)
DETRAT=DETRAT*R PCTVIS, DETRAT, PSUBK)
0 (1 = EXP(-(FL(I)*PR OP*DETRAT*DELT*FL(J)))
0 (1 = 1) = 0.0
GOTO 19 = 0.0
GOTO 10 = 0.0
GOTO 19 = 0.0
GO
```

```
MM3=LNT(1-3)

PROB=[1:0-0[1:1]+PT[1:1]*PROB

PROB=[1:0-0[1:1]+PT[1:1]*PROB

PROB=[1:0-0[1:MM1]*0[1:1]*PROB

PROB[1:3]=AFDA[1:3]+PT[1:1]*PROB

PROB[1:3]=AFDA[1:3]+PT[1:1]*PROB

PROB[1:0-0[1:MM1]*0[1:2]*PROB

PROB[1:0-0[1:MM1]*0[1:2]*PROB

PROB[1:0-0[1:MM1]*0[1:2]*PROB

PROB[1:0-0[1:MM1]*0[1:2]*PROB

PROB[1:0-0[1:MM1]*0[1:2]*PROB

PROB[1:0-0[1:MM1]*0[1:2]*PROB

PROB[1:0-0[1:MM1]*0[1:2]*PROB

PROB[1:0-0[1:MM1]*0[1:2]*PROB

PROB[1:0-0[1:MM1]*0[1:0]*PROB

PROB[1:0-0[1:0]*MM1]*0[1:0]*PROB

PROB[1:0-0[1:MM1]*0[1:0]*PROB

PROB[1:0-0[1:0]*MM1]*0[1:0]*PROB

PROB[1:0-0[1:MM1]*0[1:0]*PROB

PROB[1:0-0[1:MM1]*0[1:0]*PROB

PROB[1:0-0[1:MM1]*0[1:0]*PROB

PROB[1:0-0[1:0]*MM1]*0[1:0]*PROB[1:0-0[1:0]*MM1]*0[1:0]*PROB

PROB[1:0-0[1:MM1]*0[1:0]*PROB[1:0]*PROB[1:0]*PROB[1:0]*PROB[1:0]*PROB[1:0]*PROB
```

SUMR=0.0
SUMR=0.0
SUMB=0.0
SUMB=0.0
IF (10ST AT 11).En.2) GD TO 40
M6=NA(1)
SUMB=0.0
IF (M6 Eq.0) GD TO 47
IF (M6 Eq.0) GD TO 47
IF (M6 Eq.0) GD TO 42
IT YPE =2
IT YPE =3
IT YPE =2
IT YPE =2
IT YPE =3
IT YP

0000000

ATTRITION

```
THEO4330

THEO4340

THEO4340

THEO4340

THEO44400

THEO44400

THEO44400

THEO44400

THEO44400

THEO44400

THEO44400

THEO44500

THEO45000

THEO44500

THEO44500

THEO44500

THEO44500

THEO44500

THEO44500

THEO44500

THEO47100

THEO47100

THEO47100

THEO47100

THEO47100
                                                                                                                                                                                                                                                            itime=""I4" IX, "SEC. "/ IX, "AVERAGE RANGE BETWEEN RED
                                                                                                                                                                                                                                                                                                                                                       (6,114,11,11(1),FL(1),1UST AT (1),TPOL (1),(LOT(1,J),J=1,N6)
T(2X,11,6X,13,7X,F5.3,7X,11,6X,F5.3,5X,3(11,1X)//)
                                                                                                                                                                                                                                                                                           LOST-PCT
                                                                                                                                                                                                                                                                                            STATUS
                                                                                                                                                                                                                                                                                                                                 3,7X,F5.3,7X,11,6X,F5.3)
                                                                                                                                                                                                                                                                                           FORCE LEVEL
                                                          LOCATION
                                                                                                                                                                                                                              IF(MP.LE.4) GOTO 9

WRITE(61127)

FORMAT(11.)

WRITE(6,112)ITIME:

REUE='F6,113'IX'P'

WRITE(6,113)

FCRMAT(1X',UNIT LO
                         11 ME = I C* 10
                                                                                                                                                                                                                                                                                                           1=1,1
                                                                                                                                                                                                                                                                                                         DO 59 I=
N6=NT(I)
IF(N6.NE
WRITE(6
FORMAT(2
GOTO 59
                                                                                                                                                                                                                                                                                            113
                                                                                                                                                                                                                                                                                                                                                       48
                                                                                                                                                                                                                         125
                                                                                                                                                                                                                                               127
                                                                                                                                                                                                                                                                                                                                         264
                                                                                           57
```

CCC

```
BATTL
                                                                                                                                                                      9
                                                                                                                                                   BATTLE. )
                                                                                                          OF BATTLE. 1)
                                                                                                                                                                      CLOSE. END
                   CF LOST=', F5.3///
                                                                                                                                                   OF
          LOST=",F 5.3)
                                                                                                                                                                      100
                                                                                                                                                   END
                                                                                                          END
                                                                                                                                                                      IS
                                                                                                                                                   ELI MI NA TED.
                                                                                                          ELIMINATED.
                                                                                                                                                                      BETWEEN FORCES
          OF
                  TOTAL PERCENTAGE
          PERC EN TAGE
                                               BATTLE DETERMINATION
                                                                                                                                                   IS
                                                                                                          IS
                                                                         IOT=0

DG 53 I=1 NRJ

IF (FL(I). EQ.0.0) GGTG 53

IOT=1

ICCNTINUE

IF (IOT-EQ.1) 3D TO 54

WRITE (6.117)

7 FORMAT(IX, *** RED FORCE IS

GOTO 66

4 ICT=0

DG 55 I=K, L

ICT=0

IF (FL(I). EQ.0.0) GGTG 55

IF (IOT-EQ.1) GGTG 56

WRITE (6.118)

18 FORMAT(IX, *** BLUE FORCE

56 IF (AVD. GT.500.0) GGTG 65

WRITE (6.119)
                                                                                                                                                   FORCE
         IN TAL
          BTPOL
                                                                                                                                                                           GÍTO 66
IC=IC+1
GOTO 67
STOP
DEBUG SUBCHK
END
                                               FOR
                                               CHECK
                                                                                                                                                             56
          115
                   116
                                                                                                                                                   1 18
                                                                                                                                                                     119
                                                                                                                                                                                   65
                                                                                                          117
                                                                                                                   54
                                                                                                                                      55
                                                                                                                                                                                             99
                        UUUUUUUUUUU
                                                                                                                                                                                                           0000
```

SUBROUT INES.

COCOC

S

```
$\text{Subroutine Lamba(1) 4 PcTV1S} \text{FERAT PR} \text{PK} \text{Subroutine Lamba(1) 4 PcTV1S} \text{FORTO TOW (PCTV1S)} \text{Carbanous CRPVL Carbanous CRPVL I PROINT (6) 13 EC wD(6) 10 PcTV1S) (6) 10 PcTV1S \text{Carbanous CRPVL Carbanous CRPVL Car
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             00
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                S
```

```
SETUP
LLS/ XC(100), YC(100), PEAK(100), SX(100), SY(100), RHU(100)
LLS/ SCALE(100), TWORHO(100), TWO SCL(100), BASE
LLS/ NHILLS
                                    SUBROUTINE SORT(I,M)
COMMON /GRP 5/ LOT(6,6), ROT(6,6)
DO 19 J=1,M
I F(ROT(I,M) GE.ROT(I,J) GOTO 19
IN = LOT(I,J) = ROT(I,M)
LOT(I,M) = R
CONTINE SETUP
COMMON /HILLS/ XC(100), YC(100), PEAP
COMMON /HILLS/ SCALE(100), TWORHO(10
COMMON /HILLS/ SCALE(100), TWORHO(10)
RETURN
DEBUG SUBCHK
END
                                                                                                                         89
                                                                                                                                                                                                                                                             19
```

SOU

```
GRS, KELL, KINT
10,10), LISTH(450), KHREP(100), KTREP
10,10), LISTC(400), KCREP(150)
50 ), CPEAK(150), CPXX(150), CPYY(150)
                                                                                                                                                                                                                                                                                                                                                                                                                  (I),CPEAK(I),CPXX(I),CPYY(I),CPXY(I)
                                                                                                                                                                                 JF 8. 3 F 6. 4)
11. N F IL LS
7) XC(1), YC(1), PEAK(1), SX(1), SY(1), PHO(1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  GR ID
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 10,000
     ISTC(I), I=1,NCTOT)
HILLS
1.625
1.625
-500.)*100.
-930.)*100.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    ξ
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     ERS
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  XC(I)=(XC(I)

YC(I)=(XC(I)

XCALE(I)=[XC(I)

XCALE(I)=[XC(I)

XHREPE(I)=[XC(I)

XHREPE(I)=[XC(I)

XHREPE(I)=[XC(I)

XHREPE(I)=[XC(I)

XHREPE(I)=[XC(I)

XHRED

XHRE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           65
                                                                                                                                                                                                                                                                                                                                        37
                                                                                                                                                                                                                                                                                                                                                                                                                                      27
                                                                                                                                                                                                                                          20
                                                                                                                                                                                                                                                                                                                                                                                                                                                                           09
```

```
SUBR
         110
120
125
130
        100
```

```
TOUCH THE A TO B LINE FOR EACH SJCH ELL IPSE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         250
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  C CHECK ELEVATIONS AT SI AND 52 FOR CHECK ELEVATIONS AT SI AND 52 FOR INCVELS. EC. 0) GCTG 270

CFTMAX= 0.

I F (NCVELS. EC. 0) GCTG 270

IX = IGX (K)

I >= IGY (K)

I == IGY (K)

I == IGY (K)

I == IGY (IX)

I == I
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         C GRID
C GRID
C NOW F
                140
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 170
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             180
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           190
                                                                           150
                                                                                                                                                                                                                                                                                                                                     160
```

THE 01/2000

THE 0

```
HILL
      HHV=HHW
```

```
FCNU=2 4+H+V*(TWGCV*V+FV-1.)

FCNU=2 4+H+V*(TWGCV*V+FV-1.)

FACTOR=(TWGCV*TWGCV+2.*(GQ+TWJGV*FQ)+FSQ)

FACTOR=(TWGCV*TWGCV+2.*(GQ+TWJGV*FQ)+FSQ)

IF (ARS (DFCNV)

IF (POWER (I)*EXP (POWER)

IF (POWER (I)*EXP (POWER)

IF (ARS (DFCNV)

IF (ARS (D
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   F V=Fv=v
F WnGV=2.*GQ*V
FCNV=ZB +HHV*((FQ+TWDGV)*VM1-1.)
KN=KN+1
FACTOR=(TWDGV*TWDGV+2.*(GQ+TWDGV*FQ)+FSQ)
DFCNV=HHV*VM1*FACTOR
IF(ABS(DFCNV) -LT.1.E-10) GG TG 450
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    VMI=V-I
HFV=HHW
NCT=0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           F V=F0*V
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           C NEWT
```

330

380

```
S=-VM1

CALL KNVER (ZB, TMA CA, S IZEA, ZA, S, HTV, ZV, VISFRA)

If (VISFRA, LE, O.) GO TO 510

CON INUE

RETURN

VISFR = O.

                                                                                                                                                                                                                                                                                                  480
                                                                                                                                   HHV=PEAK(I) *EXP (POWER)
DhHV=HHV* (F C+TWOGV)
                    FV=F0*V
TMOGV=2.*G0*V
PCWER = EQ+FV+
IF(POWER .LT.
HHV=PEAK(I)*EX
                                                                                                                           L V=ZB+DHHV*1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       2000
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      510
                                                                                                                                                                                                                       450
                                                                                                                                                                                                                                                                                                                                                            480
                                                                                                                                                                                                                                                                                                                                                                                                                                                                               500
```

```
THE09610

THE09630

THE096640

THE096640

THE096640

THE096640

THE09680

THE09720

THE09720

THE09720

THE09730

THE09730

THE09730

THE09880

THE09880

THE09880

THE09880

THE09880

THE09890

THE09980
                                                           10) NHL(10) 10) LISTH(450), KHREP(100), KTREP (100), KTREP (100), NC(10, 10), LI STC (400), KCREP(150) (1000) / 1000 / AIN ELE VATI CN FOR GIVEN X, Y COORDINATES.
E( 100) , TWORH O( 100) , TWO SCL( 100) , BASE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  S 0 + 0Y S Q + Q X Y )
                                                                                                                                                                                                                                                                                                                                                    150
                             CCMMON /HILLS/ NHILLS COMMON /GRID/ LST(10,10),NHL COMMON /GRID/ LST(10,10), 
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   1*0×0×0×0
                                                                                                                                                        F UNC
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           150
                                                                                                                                                           S
```

#### APPENDIX B

## Definition of Variables in Computer Program

<pre>IPRDIR'(I)</pre>	=	Primary direction of unit i
ISECWD(I)	-	Width of search section of unit i
MVTDIR(I)	-	Movement direction of unit i
X(I),Y(I)	=	Coordinates of unit i
SPD(I)	=	Speed of unit i
TA(K)	=	Time to acquire a target for the $K^{th}$ weapon system type $(K = 1, 2)$
TI(K)	-	Time to fire first round after target acquired for the $K^{th}$ weapon system type $(K = 1, 2)$
TH(K)	-	Time to fire a round following a hit for the $K^{th}$ weapon system type $(K = 1, 2)$
TM(K)	=	Time to fire a round following a miss for the $K^{th}$ weapon system type $(K = 1, 2)$
TF1(K)	-	Projectile time of flight to 1000 m for the $K^{th}$ weapon system type $(K = 1, 2)$
TF2 (K)	-	Projectile time of flight to 2000 m for the $K^{th}$ weapon system type $(K = 1, 2)$
TF3 (K)	-	Projectile time of flight to 3000 m for the $K^{th}$ weapon system type $(K = 1, 2)$
P(I,J)	=	Probability of hit on first round.  I = unit index. J = range index  (J = 1, 2, 3, 4, 5, 6 corresponds to range  = 500, 1000, 1500, 2000, 2500, 3000 meters)
PHH(I,J)	-	Probability of a hit on a round following a hit. For I and J see P(I,J)
PHM(I,J)	-	Probability of a hit on a round following a miss. For I and J see P(I,J)

= Probability of destroying a target given PKH(I,J) it is hit NBU Number of Blue units NRU = Number of Red units FL(I) = Force level of unit i FO(I) = Initial force level of unit i = Number of intervals in the ith route NOI(I) I = 1, 2, 3= Coordinates of the center of the jth XIC(I,J), interval in the ith route YIC(I,J) = Direction of the j<sup>th</sup> interval in the i<sup>th</sup> IDIR(I,J) route AVSP Average speed of moving non-firing units IUSTAT(I) = Status of unit i does not fire ) fires destroyed Interval index for unit i II(I) no line-of-sight between unit i and unit j LOST(I,J) line-of-sight exists between unit i and unit j = Fraction of unit A (height fraction) as seen VISFRA by unit B = Fraction of unit B (height fraction) as VISFRB seen by unit A SIZETK = Height of a tank = Height of a TOW vehicle SIZETW NT(I) = Number of targets of unit i NF(I) = Number of time intervals unit i is firing continuously at the same route interval DISMAX = The maximum horizontal distance allowed between the two Red units before delaying

the faster one

NLOSC(I,J)	=	Number of continuous time intervals that line-of-sight does not exist between unit i and unit j				
VISFR(I,J)	-	The height fraction of unit i as seen by unit j				
RMINTK	=	Minimum firing range for a tank				
RMINTW	-	Minimum firing range for a TOW				
RMXTK	=	Maximum firing range for a tank				
RMXTW	=	Maximum firing range for a TOW				
TOWFR	=	Tow fire rate				
TNKFR	=	Tank fire rate				
NOD	=	Number of time intervals that a firing Red unit is delayed at the same route interval before moving to next route interval				
RF	-	Detection rate reduction factor for a firing unit (in comparison with non-firing unit)				
PM	-	The proportion of time a moving unit is busy with targets search				
PTT(I,J)	=	Proportion of the surviving firepower allocated to the i <sup>th</sup> target if there are j targets available				
LOT(I,J)	=	The number of the j <sup>th</sup> target of unit i				
ROT(I,J)	=	The range of the j <sup>th</sup> target of unit i				
POA(I,J)	=	The proportion of the j <sup>th</sup> attacker of unit i allocated to fire on unit i				
APOA(I,J)	=	The average proportion of the j <sup>th</sup> attacker of unit i allocated to fire on unit i				
LOA(I,J)	=	The number of the j <sup>th</sup> attacker of unit i				
NA(I)	=	Number of attackers of unit i				
OFL(I)	=	Force level of unit i at the previous time interval				

POL(I) = Percentage of lost of unit i during the current time interval

TPOL(I) = Total percentage of lost (since the battle began) of unit i

RTPOL = Red total percentage of lost

BTPOL = Blue total percentage of lost

# APPENDIX C SENSITIVITY ANALYSIS RESULTS CONCERNING FIRE ALLOCATION

## FIRE ALLOCATION POLICY 1

TIME 10 SEC. AVERAGE RANGE BETWEEN RED AND BLUE=3260.1 M

TIME 20 SEC. AVERAGE RANGE BETWEEN FED AND BLUE 3220.1 M

UNIT	LOCATION	FORCE LEVEL	STATUS	LOST-PCT	TARGETS
1	3	3.000	1	0.0	6
2	3	3.000	1	0.0	6
3	3	2.382	1	0.206	6
4	***	3.00C	0	0.0	
5	***	3.00C	Ō	0.0	
6	***	1.889	1	0.370	3 2 1

RED TOTAL PERCENTAGE OF LOST=0.069
BLUE TOTAL PERCENTAGE CF LOST=0.123

TIME= 30 SEC. AVERAGE RANGE BETWEEN RED AND BLUE=3220.1 M

LNI T	LOCATION	FORCE LEVEL 3.000	ST ATUS	LOST-PCT	TARGETS
3	3	1.992	î	0.336	6
5	***	3.000	0	0.0	
6 .	***	0.836 NTAGE OF LOST	-0 112	0.721	3 2
BLUE	TOTAL PERC		T=0.240		

TIME 40 SEC. AVERAGE RANGE BETWEEN RED AND RLUE=3659.7 M

UNIT	LOCAT ION	FORCE LEVEL	STATUS	LJST-PCT	TARGETS
1	3	3.000	I,	0.0	6
3	3	1.820	i	0.393	6
4	***	3.000	õ	0.0	
5	***	3. 00 C	<u>o</u>	0.0	
PED T	OTAL PERCE	NTAGE OF LOST	=0 131	1.000	3 2
ELUE	TOTAL PERC	ENTAGE OF LOS	T=0.333		

TIME= 50 SEC. AVERAGE RANGE BETWEEN FED AND BLUE=3620.1 M

LOCAT ION FORCE LEVEL ST ATUS UNIT LOST-PCT TARGETS 3.000 3.000 1.820 3.000 0.0 44 0 123 ŏ 0.393 Õ \*\*\* 0 \*\* RED TOTAL PERCENTAGE OF LOST=0.131 ELUE TOTAL PERCENTAGE OF LOST=0.333 1.000

TIME - 6C SEC. AVERAGE RANGE BETWEEN RED AND BLUE = 3580.6 M

LOST-PCT FORCE LEVEL 3.000 3.000 LOCATION STA TUS UNIT TARGETS 00 555 1.82C 3.000 3.000 0.393 0 45 \*\*\* 0 \*\*\* RED TOTAL PERCENTAGE OF LOST=0.131
BLUE TOTAL PERCENTAGE CF LOST=0.333 1.000

TIME 70 SEC. AVERAGE RANGE BETWEEN RED AND BLUE=3541.0 M

TIME - 8C SEC. AVERAGE RANGE BET EEN RED AND BLUE = 3501.5 M

TIME = 90 SEC. AVERAGE RANGE BETWEEN RED AND BLUE=3462.0 M

LOST-PCT 0.198 0.0 0.393 LOCATION FORCE LEVEL UN IT STATUS TARGETS 2.406 3.000 1.820 2.751 3.000 888 10 ŏ \*\*\* 0.083 1 \*\*\* 0.0 RED TOTAL PERCENTAGE OF LOST=0.197
BLUE TOTAL PERCENTAGE OF LOST=0.361 1.000

TIME = 100 SEC. AVERAGE RANGE BETWEEN RED AND BLUE = 3435.6 M

LNIT LOCATION FORCE LEVEL STATUS LCST-FCT TARGETS

1 8 1.861 1 0.380 4

2 9 3.000 0 0.0

3 9 1.820 0 0.393

4 \*\*\* 2.558 1 0.147 1

5 \*\*\* 3.000 0 0.0

6 \*\*\* 0.0 2 1.000

RED TOTAL PERCENTAGE OF LOST=0.258
BLUE TOTAL PERCENTAGE CF LOST=0.382

TIME 110 SEC. AVERAGE RANGE BETWEEN RED AND BLUE 3409.3 M

TIME= 12C SEC. AVERAGE PANGE BETWEEN RED AND BLUE=3369.8 M

UNIT LOCATION FORCE LEVEL STATUS LOST-PCT TARGETS

1 9 0.874 1 0.709 4

2 11 3.000 0 0.0

3 11 1.820 0 0.353

4 \*\*\* 2.327 1 0.224 1

5 \*\*\* 3.00C 0 0.0

RED TOTAL PERCENTAGE OF LOST=0.367
BLUE TOTAL PERCENTAGE OF LOST=0.408

TIME= 130 SEC. AVERAGE RANGE BETWEEN RED AND BLUE=3343.5 M

UNIT	LOCAT ION	FORCE LEVEL	STATUS	LOST-PCT	TARGETS
1	. 9	0.412	1	0.863	4
2	12	3. 00C	1	0.0	4
4	***	1.820	ĭ	0.342	1 2
5	***	3.000	Ō	0.0	
6	***	0.0	ž	1.000	
RED 1	TOTAL PERCE	NTAGE OF LOST	=0.419		
BLUE	TOTAL PERC	ENTAGE OF LOS	T=0.447		

TIME= 140 SEC. AVERAGE PANGE BETWEEN RED AND BLUE=3343.5 M

TIVU	LOCATION	FORCE LEVEL	STA TUS	LOST-PCT 0.993	TARGETS
4	12	3.000 1.82C	ò	0.393	*
4	***	1.660	ĭ	0.447	1 2
5	***	3.000	g	0.0	
RED T	OTAL PERCE	NTAGE OF LOST	=0 -462	1.000	
BLUE		ENTAGE CF LOS			

TIME= 150 SEC. AVERAGE RANGE BETWEEN RED AND BLUE=3334.3 M

LNIT	LOCATION	FORCE LEVEL	ST ATUS	LOST-PCT	TARGETS
1 2	10	3.000	2	1.000	4
3	13	1.820	Õ	0.393	
5	***	1.349	0	0.550	1 2
6 .	***	0.0	2	1.000	
BLUE	TOTAL PERC	NTAGE OF LOST ENTAGE OF LOS	T=0.464		

TIME 160 SEC. AVERAGE RANGE BETWEEN FED AND BLUE 3295.5 M

UNIT	LOCATION	FORCE LEVEL	STATUS	LOST-PCT	TARGETS
2	13	2.732	1	1.000 0.089	4
4	***	1.820	0	0.393	2
5	***	3.000 0.0	0	0. C 1.000	
RED T	TOTAL PERCE		=0.494 T=0.548		

TIME= 170 SEC. AVERAGE RANGE BETWEEN RED AND BLUE=3276.1 M

FORCE LEVEL 0.0 2.521 1.820 0.804 LNIT LOCATION ST ATUS LOST-PCT TAR GETS 10 1.000 210 1234 0.160 0.393 0.732 4 15 \*\*\* 2 5 \*\*\* 3.000 0 6 \*\*\* RED TOTAL PERCENTAGE OF LOST=0.518 ELUE TOTAL PERCENTAGE CF LOST=0.577 0.0 1.000

TIME 180 SEC. AVERAGE RANGE BETWEEN RED AND BLUE 3256.6 M

LOST-PC T 1.000 0.213 0.393 0.813 LOCATION FORCE LEVEL UNIT STATUS TARGETS 10 0.0 2.361 1.820 0.560 3.000 210 123 4 16 IO 2 \* \* \* 0.0 6 \*\*\* 0.0

RED TOTAL PERCENTAGE OF BLUE TOTAL PERCENTAGE OF \*\*\* RED 1.000 OF LOST = 0.535 OF LOST = 0.604

TIME= 19C SEC. AVERAGE RANGE BETWEEN RED AND BLUE=3217.8 M

TIME = 200 SEC. AVERAGE RANGE BETWEEN RED AND BLUE=3217.8 M

TIME = 21 C SEC. AVERAGE RANGE BETWEEN RED AND BLUE = 3623.1 M

LOST-PCT 1.000 0.279 0.393 1.000 LOCATION FORCE LEVEL STA TUS TARGETS UNIT 10 14 17 2 0.0 2.164 4 34 1.82C 020 2 \*\*\* 5 \*\*\* 3.000 0 6 \*\*\* 0.0 2 RED TOTAL PERCENTAGE OF LOST=0.557 BLUE TOTAL PERCENTAGE OF LOST=0.667 1.000

TIME= 220 SEC. AVERAGE RANGE BETWEEN RED AND BLUE=3583.1 M

UNIT LOCATION FORCE LEVEL STATUS LOST-PCT TARGETS
1 10 0.0 2 1.00C
2 15 2.164 0 0.279
3 18 1.82C 0 0.393
4 \*\*\* 0.0 2 1.000
5 \*\*\* 0.0 2 1.000
6 \*\*\* 0.0 2 1.000
RED TOTAL PERCENTAGE OF LOST=0.557
BLUE TOTAL PERCENTAGE CF LOST=0.667

TIME= 230 SEC. AVERAGE RANGE BETWEEN FED AND BLUE=3543.2 M

LOCAT ION TIAU FORCE LEVEL ST ATUS LOST-PCT TARGETS 20 1.000 0.279 0.393 1.000 0.0 2.164 1.820 3.00C 10 16 19 123 ŏ \*\*\* ō 5 \*\*\* 0.0 1.000 RED TOTAL PERCENTAGE OF LOST=0.557
BLUE TOTAL PERCENTAGE OF LOST=0.667

TIME= 24C SEC. AVERAGE RANGE BETWEEN RED AND BLUE=3503.2 M

TIME= 250 SEC. AVERAGE RANGE BETWEEN RED AND BLUE=3463.3 M

TI ME = 260 SEC. AVERAGE RANGE BETWEEN RED AND BLUE=3423.3 M

TIME 270 SEC. AVERAGE RANGE BETWEEN FED AND BLUE 3383.3 M

TIME= 28C SEC. AVERAGE RANGE BETWEEN RED AND BLUE=3343.4 M

TIME= 290 SEC. AVERAGE RANGE BETWEEN RED AND BLUE=3303.4 M

TIME = 300 SEC. AVERAGE RANGE BETWEEN RED AND BLUE=3263.4 M

UNIT LOCATION FORCE LEVEL STATUS LCST-FCT TARGETS

1 0 0.0 2 1.000
2 23 2.164 0 0.279
3 26 1.820 0 0.393
4 \*\*\* 0.0 2 1.000
5 \*\*\* 3.000 0 0.0
6 \*\*\* 0.0 2 1.000

RED TOTAL PERCENTAGE OF LOST=0.557
BLUE TOTAL PERCENTAGE CF LOST=0.667

TIME= 310 SEC. AVERAGE RANGE BETWEEN FED AND BLUE=3223.5 M

UNIT LOCATION FORCE LEVEL STATUS LOST-PCT TARGETS

1 10 0.0 2 1.000
2 24 2.164 0 0.279
3 27 1.820 0 0.393
4 \*\*\* 0.0 2 1.000
5 \*\*\* 0.0 2 1.000
6 \*\*\* 0.0 2 1.000
RED TOTAL PERCENTAGE OF LOST=0.557
BLUE TOTAL PERCENTAGE OF LOST=0.667

TIME= 32 C SEC. AVERAGE RANGE BETWEEN RED AND BLUE=3183.5 M

TIME= 330 SEC. AVERAGE RANGE BETWEEN RED AND BLUE=3143.6 M

TI ME = 340 SEC. AVERAGE RANGE BETWEEN RED AND BLUE=3103.6 M

TIME 350 SEC. AVERAGE RANGE BETWEEN RED AND BLUE 3063.7 M

TIME= 36C SEC. AVERAGE PANGE BETWEEN RED AND BLUE=3023.7 M

TIME= 370 SEC. AVERAGE RANGE BETWEEN RED AND RLUE=3003.7 M

UNIT	LOCAT ION	FORCE LEVEL	STATUS	LOST-PCT	TARGETS
2	30	2.164	Ō	0.279	
3	32	0.656	1	0.781	5
4	***	0.0	2	1.000	
5	***	2.805	1	0.065	3
-6	***		2	1.000	
RED T	UTAL PERCE	NTAGE OF LOST	=0.687		
BLUE	IUIAL PERC	ENTAGE OF LOS	T=0.688		

TI ME = 380 SEC. AV ERAGE RANGE BETWEEN RED AND BLUE = 2983.8 M

LNIT	LOCATION	FORCE LEVEL	STATUS	LOST-PCT	TARGETS
2	31	2.164	Ó	0.279	
3	32	C. 10C	i	0.967	5
4	***	0.0	2	1.000	
5	***	2.795	1	0.068	3
_6	***	0.0	2	1.000	
FED T	OT AL PERCE	NTAGE OF LOST	=0.748		
BLUE	TUTAL PERC	ENTAGE CF LOS	T=0.689		

TIME= 390 SEC. AVERAGE RANGE BETWEEN FED AND BLUE=2961.7 M

ETS
3

TIME = 400 SEC. AVERAGE RANGE BETWEEN RED AND BLUE = 2961.7 M

UNIT	LOCAT ION	FORCE LEVEL	STATUS	LOST-PCT	TARGETS
2	32	1.654	1	0.449	5
34	***	0.0	2	1.000	
6	***	2.399	2	0.200	2
RED T	TOTAL PERCE	NTAGE OF LOST Entage of Los	=0.816 T=0.733		

TIME= 410 SEC. AVERAGE RANGE BETWEEN FED AND BLUE=2961.7 M

UNIT	LOCATION	FORCE LEVEL	ST ATUS	LOST-PCT	TARGETS
2	32	1.178	1	1.000 0.607	5
4	33 ***	0.0 0.0 2.277	2	1.000	
5	***	0.0	1 2	0.241	2
RED T	TOTAL PERCE	NTAGE OF LOST ENTAGE OF LOS	=0.869 T=0.747		

TIME= 42 C SEC. AV ERAGE RANGE BETWEEN RED AND 3LUE=2921.7 M

TINU	LOCATION	FORCE LEVEL	STA TUS	LOST-PCT	TARGETS
2	33	0.724	i	0.759	5
3	33 ***	0.0	2	1.000	
5	*** ***	2. 20 2	1 2	0.266	2
RED T	OTAL PERCE	NTAGE OF LOST ENTAGE CF LOS	=0.920 T=0.755	1.000	

TIME= 430 SEC. AVERAGE RANGE BETWEEN RED AND BLUE=2921.7 M

UNIT	LOCATION	FORCE LEVEL	STATUS	LOST-PCT	TARGETS
2 2	10 33 33	0.0 0.286 0.0	1 2	1.000 0.905 1.000	5
4 5	***	C. 0 2.172	2	1.000	2
RED TO	TAL PERCE	O.O NTAGE OF LOST ENTAGE CF LOS	2 = 0. 968 T=0.759	1.000	

TIME= 440 SEC. AVERAGE RANGE BETWEEN RED AND BLUE=2921.7 M

UNIT	LOCATION	FORCE LEVEL	STATUS	LOST-PCT	TARGETS
2	33	0.0	2	1.000	5
4	***	0.0	2	1.000	
5	***	2.172	1 2	0.276	2
REDT	TOTAL PERCE	NTAGE OF LOST	=1.000 T=0.759		

\*\*\* RED FORCE IS ELIMINATED. END OF BATTLE.

## FIRE ALLOCATION POLICY 2

TIME= 10 SEC. AVERAGE RANGE BETWEEN RED AND BLUE=3260.1 M

LNIT	LOCATION	FORCE LEVEL	STATUS	LOST-FCT	TARGETS
1	2	3. 00C	0	0.0	
2	2	3.00C	0	0.0	
3	2	3.000	Ó	0.0	
4	***	3. 00C	0	0.0	
5	***	3.000	0	0.0	
6	***	3.000	0	0.0	
RED T	OTAL PERCE	NTAGE OF LOST	=0.0		
BLUE	TOTAL PERC	ENTAGE CF LOS	T=0.0		

TIME= 20 SEC. AVERAGE RANGE BETWEEN RED AND RLUE=3220.1 M

UNIT	LOCATION	FORCE LEVEL	STATUS	LOST-PCT	TARGETS
1	3	2.97C	1	0.010	6
2	3	2.908	1	0.031	6
3	3	2.505	1	0.165	6
4	***	3.000	Ō	0.0	
5	***	3-000	Ŏ	0 - C	
6	***	1.887	i	0.371	3 2 1

RED TOTAL PERCENTAGE OF LOST=0.068
BLUE TOTAL PERCENTAGE OF LOST=0.124

TIME 30 SEC. AVERAGE RANGE BETWEEN FED AND BLUE=3220.1 M

UNIT	LOCATION	FORCE_LEVEL	STATUS	LOST-PCT	TAR GETS
1	3	2.951	Ţ	0.016	6
2	3	2.851	į	0.050	6
3	***	2.194	Ţ	0.269	6
2	***	3.000	ŏ	0.0	
2	***	0-832	1	0.723	2 2 1
0	T T-4	0.032		0 -123	2 4 1

REC TOTAL PERCENTAGE OF LOST=0.112 BLUE TOTAL PERCENTAGE CF LOST=0.241

TIME= 40 SEC. AVERAGE RANGE BETWEEN RED AND BLUE=3659.7 M

LNIT	LOCATION	FORCE LEVEL	ST ATUS	LOST-PCT	TAR GETS
ī	3	2- 943	į	0.019	6
2	3	2.827	1	0.314	2
4	***	3.000	ō	0.014	0
5	***	3.000	Ŏ	0.0	
6	***	0.0	2	1.000	3 2 1

RED TOTAL PERCENTAGE OF LOST=0.131
BLUE TOTAL PERCENTAGE OF LOST=0.333

TIME= 50 SEC. AVERAGE RANGE BETWEEN RED AND BLUE=3620.1 M

TIME = 60 SEC. AVERAGE RANGE BETWEEN RED AND BLUE=3580.6 M

TIME 70 SEC. AVERAGE RANGE BETWEEN RED AND BLUE=3541.0 M

TIME= 8C SEC. AVERAGE RANGE BETWEEN RED AND BLUE=3501.5 M

TIME 9C SEC. AVERAGE RANGE BETWEEN RED AND BLUE = 3462.0 M

FORCE LEVEL 2.349 2.825 2.057 2.757 3.000 LOST-PCT 0.217 0.058 0.314 0.081 LOCATION UNIT STA TUS TARGETS 88 0 8 0 \*\*\* 1 0.0 \*\*\* FED TOTAL PERCENTAGE CF LOST=0.197
BLUE TOTAL PERCENTAGE CF LOST=0.360 1.000

TIME= 100 SEC. AVERAGE RANGE BETWEEN RED AND BLUE=3435.6 M

FORCE LEVEL 1.803 2.825 2.057 2.570 3.000 LOST-PCT 0.399 0.058 LOCATION ST ATUS LNIT TARGETS 899 1 ō 0.143 ŏ \*\*\* 1 5 \*\*\* 0.0 RED TOTAL PERCENTAGE OF LOST=0.257
BLUE TOTAL PERCENTAGE CF LOST=0.381 1.000

TIME = 110 SEC. AVERAGE RANGE BETWEEN RED AND BLUE = 3409.3 M

FORCE LEVEL 1.294 2.825 2.057 2.436 3.000 LOST-PCT 0.569 0.058 0.314 UNIT LOCAT ION STATUS TARGETS 10 000 23 \*\*\* 0.188 1 \*\*\* 02 6 \*\*\*
RED TOTAL PERCENTAGE OF LOST=0.314
BLUE TOTAL PERCENTAGE OF LOST=0.396 1.000

TI ME = 120 SEC. AVERAGE PANGE BETWEEN RED AND BLUE = 3369.8 M

LCST-FCT 0.730 0.058 0.314 0.216 0.0 LOCATION FORCE LEVEL STATUS LNIT TARGETS 0.810 2.825 2.057 2.352 10 12345 0 \*\*\* 1 \*\*\* 3.000 0 RED TOTAL PERCENTAGE OF LOST=0.368
BLUE TOTAL PERCENTAGE CF LOST=0.405 1.000

TIME= 130 SEC.
AVERAGE RANGE BETWEEN RED AND BLUE=3343.5 M

LOST-PCT 0.855 0.089 UNIT LOCATION FORCE LEVEL STA TUS TARGETS 0.436 2.732 2.057 2.023 12 123 0.314 0.326 0.0 0 \*\* 1 2 \*\*\* 6 \*\*\*
RED TOTAL PERCENTAGE OF LOST=0.419
BLUE TOTAL PERCENTAGE OF LOST=0.442 1.000

TIME = 140 SEC. AVERAGE RANGE BETWEEN RED AND BLUE = 3343.5 M

FORCE LEVEL 0.115 2.652 2.057 1.736 LOCATION 12 12 LOST - FCT 0. 962 UNIT STATUS TARGETS 123 0.116 0.314 0.421 0.000 4 Õ \*\*\* 1 2 \*\*\* 3.000 1.000 RED TOTAL PERCENTAGE OF LOST=0.464
BLUE TOTAL PERCENTAGE CF LOST=0.474 \*\*\*

TIME = 150 SEC. AVERAGE RANGE BETWEEN RED AND BLUE=3334.3 M

TIME= 160 SEC. AVERAGE RANGE BETWEEN RED AND BLUE=3295.5 M

TIME= 170 SEC. AVERAGE RANGE BETWEEN RED AND BLUE=3276.1 M

LOST-PCT 1.000 0.318 0.314 LNIT LOCATION FORCE LEVEL ST ATUS TAR GETS 0. 0 2.047 2.057 1.019 10 210 \*\* 0.660 2 \*\* 0.0 RED TOTAL PERCENTAGE OF LOST=0.544 BLUE TOTAL PERCENTAGE CF LOST=0.553 1.000

TIME= 180 SEC . AVERAGE RANGE BETWEEN RED AND RLUE=3256.6 M

UNIT LOCATION FORCE LEVEL STATUS LOST-PCT TARGETS

1 10 0.0 2 1.000
2 13 1.845 1 0.385 4
3 16 2.057 0 0.314
4 \*\*\* 0.828 1 0.724 2
5 \*\*\* 3.000 0 0 0.0
6 \*\*\* 0.0 2 1.000

RED TOTAL PERCENTAGE OF LOST=0.566
BLUE TOTAL PERCENTAGE OF LOST=0.575

TIME = 19C SEC. AVERAGE RANGE BETWEEN RED AND BLUE = 3217.8 M

UNIT LOCATION FORCE LEVEL STA TUS LOST-PCT TARGETS 10 14 17 1.000 0.0 1.680 0.440 0.314 0.782 4 0 0.654 2 5 \*\*\* 3.00C 0
6 \*\*\*
RED TOTAL PERCENTAGE OF LOST=0.585
BLUE TOTAL PERCENTAGE OF LOST=0.594 1.000

TIME = 200 SEC. AVERAGE RANGE BETWEEN RED AND BLUE=3217.8 M

TIME= 21C SEC. AVERAGE PANGE BETWEEN RED AND BLUE=3217.8 M

LOST-PCT 1.000 0.516 0.314 0.886 FORCE LEVEL UNIT LOCATION STA TUS TARGETS 0.0 1.452 2.057 0.342 10 14 17 12 4 3 ō \*\* 2 \*\*\* 0.0 6 \*\*\* 0.0 2

RED TOTAL PERCENTAGE OF LOST=0.610

BLUE TOTAL PERCENTAGE OF LOST=0.629 1.000

TIME= 220 SEC. AVERAGE RANGE BETWEEN RED AND BLUE=3179.1 M

TIME= 230 SEC. AVERAGE RANGE BETWEEN FED AND BLUE=3179.1 M

TIME= 240 SEC. AVERAGE RANGE BETWEEN RED AND BLUE=3583.1 M

FORCE LEVEL 0.0 1.332 2.057 0.0 3.00C STATUS 2 1 0 2 LOST-PCT 1.000 0.556 0.314 UNIT LOCAT ION TARGETS 10 15 18 123 4 \*\* 1.000 2 \*\*\* 0.0 6 \*\*\*

RED TOTAL PERCENTAGE OF LOST=0.623
BLUE TOTAL PERCENTAGE OF LOST=0.667 1.000

NAVAL POSTGRADUATE SCHOOL MONTEREY CA
OPERATIONAL LANCHESTER-TYPE MODEL OF SMALL UNIT LAND COMBAT. (U)
SEP 79 J SMOLER AD-A078 265 UNCLASSIFIED 2 OF 2 END DATE 1-80 DDC

TIME= 250 SEC. AVERAGE RANGE BETWEEN FED AND BLUE=3543.2 M

TIME= 260 SEC. AVERAGE RANGE BETWEEN RED AND BLUE=3503.2 M

TIME = 270 SEC. AVERAGE PANGE BETWEEN RED AND BLUE = 3463.3 M

TIME= 280 SEC. AVERAGE RANGE BETWEEN FED AND BLUE=3423.3 M

UNIT LOCATION FORCE LEVEL STATUS LOST-PCT TARGETS

1 10 0.0 2 1.000
2 19 1.332 0 0.556
3 22 2.057 0 0.314
4 \*\*\* C.0 2 1.000
5 \*\*\* 3.000 0 0.0
6 TOTAL PERCENTAGE OF LOST=0.623
BLUE TOTAL PERCENTAGE OF LOST=0.667

TIME= 290 SEC. AVERAGE RANGE BETWEEN RED AND BLUE=3383.3 M

TIME= 300 SEC. AVERAGE RANGE BETWEEN RED AND BLUE=3343.4 M

UNIT LOCATION FORCE LEVEL STATUS LOST-PCT TARGETS
1 10 0.0 2 1.000
2 21 1.332 0 0.556
3 24 2.057 0 0.314
4 \*\*\* 0.0 2 1.000
5 \*\*\* 3.00C 0 0.0
6 \*\*\* 0.0 2 1.00C

RED TOTAL PERCENTAGE OF LOST=0.623
BLUE TOTAL PERCENTAGE OF LOST=0.667

TI ME= 310 SEC. AVERAGE RANGE BETWEEN RED AND BLUE=3303.4 M

TIME= 320 SEC. AVERAGE RANGE BETWEEN FED AND BLUE=3263.4 M

TIME= 330 SE(. AVERAGE RANGE BETWEEN FED AND BLUE=3223.5 M

TIME= 340 SEC. AVERAGE RANGE BETWEEN RED AND RLUE=3183.5 M

TI ME = 350 SEC. AVERAGE RANGE BETWEEN RED AND BLUE=3143.6 M

TIME 360 SEC. AVERAGE RANGE BETWEEN RED AND BLUE 3103.6 M

LOST-PCT 1.000 0.556 0.314 1.000 LOCATION 10 27 30 FORCE LEVEL UNIT STATUS TARGETS 20 0.0 1.332 2.057 0.0 ONO \*\* \*\*\* 3.000 0.0 RED TOTAL PERCENTAGE OF LOST=0.623 BLUE TOTAL PERCENTAGE OF LOST=0.667 1.000

TIME= 370 SEC. AVERAGE RANGE BETWEEN RED AND BLUE=3063.7 M

TIME= 380 SEC. AVERAGE RANGE BETWEEN RED AND BLUE=3023.7 M

UN IT LOCAT ION FORCE LEVEL STATUS LOST-PCT TARGETS 0.0 1.332 1.462 0.0 2.84 £ 1.000 0.556 0.513 1.000 10 29 32 123 20121 5 \*\*\* 5 \*\*\* 0.051 3 RED TOTAL PERCENTAGE OF LOST=0.690
BLUE TOTAL PERCENTAGE OF LOST=0.684 1.000

TIME= 390 SEC. AVERAGE RANGE BETWEEN RED AND BLUE=3003.7 M

TIME= 400 SEC. AVERAGE RANGE BETWEEN RED AND BLUE=2983.8 M

TIME= 410 SEC. AVERAGE RANGE BETWEEN RED AND BLUE=2961.7 M

UNIT	LOCATION	FORCE LEVEL	STATUS	LOST-PCT	TARGETS
2	32	1.224	1	1.000 0.592	5
4	33 ***	0.0	2	1.000	,
5	***	2.592	1 2	0.136	3 2
RED T	TOTAL PERCE		=C.864 T=0.712		

TIME = 42 C SEC. AVERAGE RANGE BETWEEN RED AND BLUE = 2961.7 M

UNIT	LOCATION	FORCE LEVEL	STATUS	LOST-PCT	TARGETS
2	32	0.0	i	1.000	5
3	33	0.0	2	1.000	
5	***	2.519	1	1.000	2
6	***	0.0	2	1.000	
BLUE	TOTAL PERC	NTAGE OF LOST ENTAGE OF LOS	=0.921 T=0.720		

TIME = 430 SEC. AVERAGE RANGE BETWEEN RED AND BLUE=2961.7 M

LNIT	LOCATION	FORCE LEVEL	STATUS	LOST-PCT	TARGETS
2	32	0.209	1 2	0.930	5
45	***	0.0	2	1.000	2
SED T	***	0.0	=0.977	1.000	
BLUE	TOTAL PERC	ENTAGE CE LOS	T=0 -723		

TIME = 440 SEC. AVERAGE RANGE BETWEEN RED AND BLUE = 2961.7 M

LNIT	LOCATION	FORCE LEVEL	ST ATUS	LOST-PCT	TARGETS
2	33	0.0	2	1.000 1.000 1.000	5
4	***	0.0	2	1.000	2
RED T	***	0.0	T=1.000	1.000	
BLUE	TOTAL PERC	NTAGE OF LOS	ST=0.723		

\*\*\* RED FORCE IS ELIMINATED. END OF BATTLE.

#### FIRE ALLOCATION POLICY 3

TIME= 1C SEC. AVERAGE RANGE BETWEEN RED AND BLUE=3260.1 M

TIME = 20 SEC. AVERAGE RANGE BETWEEN RED AND BLUE=3220.1 M

UNIT	LOCATION	FORCE LEVEL	STATUS	LOST-PCT	TAR GETS
2	3	2.796	į	0.068	6
4	***	2.794 3.000	Ö	0.069	6
5	***	3.000	Ŏ	0.0	
6	***	1.875	1	0.374	3 2 1

RED TOTAL PERCENTAGE OF LOST=0.068 BLUE TOTAL PERCENTAGE OF LOST=0.125

TIME = 30 SEC. AVERAGE RANGE BETWEEN RED AND BLUE = 3220.1 M

LNIT	LOCATION	FORCE LEVEL	STATUS	LOST-PCT	TARGETS
2	3	2.669	i	0.110	6
3	3	2. 665	ĩ	0.112	6
4	***	3.00C	0	0.0	
5	***	3.000	0	0.0	
6	***	C. 805	1	0.730	3 2 1

RED TOTAL PERCENTAGE OF LOST=0.110 ELUE TOTAL PERCENTAGE OF LOST=0.243

TIME - 4C SEC. AVERAGE RANGE BETWEEN RED AND RLUE=3659.7 M

UN IT	LOCATION	FORCE LEVEL	STATUS	LOST-PCT	TARGETS
ī	3	2.621	1	0.126	6
2	3	2.616	1	0.129	6
4	***	3.000	ō	0.0	•
5	***	3.000	Ö	0.0	
6	***	0.0	2	1.000	3 2 1

RED TOTAL PERCENTAGE OF LOST=0.128 ELUE TOTAL PERCENTAGE CF LOST=0.333 TIME= 50 SEC. AVERAGE RANGE BETWEEN RED AND BLUE=3620.1 M

TIME 60 SEC. AVERAGE RANGE BETWEEN RED AND BLUE=3580.6 M

TIME = 7C SEC. AVERAGE RANGE BETWEEN RED AND BLUE = 3541.0 M

TIME 80 SEC. AVERAGE RANGE BETWEEN RED AND BLUE 3501.5 M

TIME= 90 SEC. AVERAGE RANGE BETWEEN RED AND BLUE=3462.0 M

UNIT LOCATION FORCE LEVEL STATUS LOST-PCT TARGETS

1 8 2.026 1 0.325 4

2 8 2.614 0 0.129

3 8 2.610 0 0.130

4 \*\*\* 2.79C 1 0.070 1

5 \*\*\* 3.00C 0 0.07

6 \*\*\* 0.0 2 1.000

RED TOTAL PERCENTAGE OF LOST=0.194
BLUE TOTAL PERCENTAGE OF LOST=0.357

TIME = 100 SEC. AVERAGE RANGE BETWEEN RED AND BLUE = 3435.6 M

TIME = 110 SEC. AVERAGE RANGE BETWEEN RED AND BLUE = 3409.3 M

UNIT LOCATION FORCE LEVEL STATUS LCST-FCT TARGETS

1 8 0.952 1 0.683 4

2 10 2.614 0 0.129

3 10 2.610 0 0.130

4 \*\*\* 2.539 1 0.154 1

5 \*\*\* 3.000 0 0.0

RED TOTAL PERCENTAGE OF LOST=0.314

BLUE TOTAL PERCENTAGE CF LOST=0.385

TIME= 120 SEC. AVERAGE RANGE BETWEEN RED AND BLUE=3369.8 M

UNIT LOCATION FOPCE LEVEL STATUS LOST-PCT TARGETS

1 9 0.447 1 3.851 4

2 11 2.614 0 0.129

3 11 2.610 0 0.130

4 \*\*\* 2.492 1 0.169 1

5 \*\*\* 3.000 0 0.0

6 \*\*\* 0.0

RED TOTAL PERCENTAGE OF LOST=0.370

BLUE TOTAL PERCENTAGE OF LOST=0.390

TIME= 130 SEC. AVERAGE RANGE BETWEEN RED AND BLUE=3343.5 M

UNIT LOCATION FORCE LEVEL STATUS LOST-PCT TARGETS

1 9 0.20C 1 0.933 4
2 12 2.367 1 0.211 4
3 12 2.610 0 0.130
4 \*\*\* 2.226 1 0.258 1 2
5 \*\*\* 3.000 0 0.0
6 \*\*\* 0.0 2 1.000

RED TOTAL PERCENTAGE OF LOST=0.425
BLUE TOTAL PERCENTAGE CF LOST=0.419

TIME 140 SEC. AVERAGE RANGE BETWEEN RED AND BLUE 3353.8 M

TIME = 15C SEC. AVERAGE RANGE BETWEEN RED AND RLUE=3334.3 M

TIME= 160 SEC. AVERAGE RANGE BETWEEN RED AND BLUE=3295.5 M

TIME= 170 SEC. AVERAGE PANGE BETWEEN RED AND BLUE=3276.1 M

TIME= 180 SEC. AVERAGE RANGE BETWEEN RED AND BLUE=3256.6 M

UNIT LOCATION FORCE LEVEL STATUS LOST-PCT TARGETS

1 9 0.0 2 1.000
2 13 0.744 1 0.752 4
3 16 2.61C 0 0.130
4 \*\*\* 1.492 1 0.503 2
5 \*\*\* 3.000 0 0.0
6 \*\*\* C.0 2 1.000
FED TOTAL PERCENTAGE OF LOST=0.627
BLUE TOTAL PERCENTAGE CF LOST=0.501

TIME= 190 SEC. AVERAGE RANGE BETWEEN FED AND BLIJE=3217.8 M

TIME = 200 SEC. AVERAGE RANGE BETWEEN RED AND BLUE = 3217.8 M

UNIT LOCATION FORCE LEVEL STATUS LOST-PCT TARGETS

1 9 0.0 2 1.000
2 14 0.159 1 0.947 4
3 17 2.610 0 0.130
4 \*\*\* 1.429 1 0.524 2
5 \*\*\* 3.000 0 0.0
6 \*\*\* 0.0 2 1.000

RED TOTAL PERCENTAGE OF LOST=0.692
BLUE TOTAL PERCENTAGE OF LOST=0.508

TIME= 210 SEC. AVERAGE RANGE BETWEEN FED AND BLUE=3231.1 M

UNIT LOCATION FORCE LEVEL STATUS LOST-PCT TARGETS

1 9 0.0 2 1.000 4

3 17 2.61 0 0 0.130

4 \*\*\* 1.425 1 0.524 2

5 \*\*\* 3.000 0 0.0

6 \*\*\* 0.0 2 1.000

RED TOTAL PERCENTAGE OF LOST=0.710

BLUE TOTAL PERCENTAGE OF LOST=0.508

TIME= 220 SEC. AVERAGE RANGE BETWEEN RED 4ND BLUE=3193.2 M

UNIT LOCATION FORCE LEVEL STATUS LOST-PCT TARGETS

1 9 0.0 2 1.000
2 14 0.0 2 1.000
3 18 2.610 0 0.130
4 \*\*\* 1.429 0 0.524
5 \*\*\* 3.00C 0 0.0
6 \*\*\* 0.0
RED TOTAL PERCENTAGE OF LOST=0.710
BLUE TOTAL PERCENTAGE OF LOST=0.508

TI ME = 230 SEC. AVERAGE RANGE BETWEEN RED AND BLUE = 3155.4 M

LNIT LOCATION FORCE LEVEL STATUS LCST-PCT TARGETS

1 9 0.0 2 1.000
2 14 0.0 2 1.000
3 19 2.327 1 0.224 4
4 \*\*\* 1.188 1 0.604 3
5 \*\*\* 3.00C 0 0.0
RED TOTAL PERCENTAGE OF LOST=0.741
BLUE TOTAL PERCENTAGE CF LOST=0.535

TIME= 240 SEC. AVERAGE RANGE BETWEEN PED AND BLUE=3155.4 M

UNIT LOCATION FORCE LEVEL STATUS LOST-PCT TARGETS

1 9 0.0 2 1.000
2 14 0.0 2 1.000
3 19 2.091 1 0.303 4
4 \*\*\* 0.571 1 0.676 3
5 \*\*\* 3.000 0 0.0
6 \*\*\* 0.0 2 1.000

RED TOTAL PERCENTAGE OF LOST=0.768
BLUE TOTAL PERCENTAGE CF LOST=0.559

TI ME = 250 SEC. AVERAGE RANGE BETWEEN RED AND BLUE = 3155.4 M

UNIT LOCATION FORCE LEVEL STATUS LCST-PCT TARGETS

1 9 0.0 2 1.000
2 14 0.0 2 1.000
3 19 1.899 1 0.367 4
4 \*\*\* 0.774 1 0.742 3
5 \*\*\* 3.000 0 0.0
6 \*\*\* 0.0 2 1.000
PED TOTAL PERCENTAGE OF LOST=0.789
BLUE TOTAL PERCENTAGE CF LOST=0.581

TIME= 260 SEC. AVERAGE RANGE BETWEEN FED AND BLUE=3117.7 M

TIME= 270 SEC. AVERAGE RANGE BETWEEN RED AND RLUE=3117.7 M

TIME= 280 SEC. AVERAGE RANGE BETWEEN RED AND BLUE =3117.7 M

UNIT LOCATION FORCE LEVEL STATUS LOST-PCT TARGETS

1 9 0.0 2 1.000

2 14 0.0 2 1.000

3 20 1.543 1 0.486 4

4 \*\*\* 0.265 1 0.912 3

5 \*\*\* 3.000 0 0.0

6 \*\*\* C.0 2 1.000

FED TOTAL PERCENTAGE OF LOST=0.829

BLUE TOTAL PERCENTAGE OF LOST=0.637

TIME= 29C SEC. AVERAGE PANGE BETWEEN RED AND BLUE=3080.0 M

TIME= 300 SEC. AVERAGE RANGE BETWEEN RED AND BLUE=3423.4 M

LNIT LOCATION FORCE LEVEL STATUS LOST-PCT TARGETS

1 9 0.0 2 1.000
2 14 0.0 2 1.000
3 21 1.468 1 0.511 4
4 \*\*\* 0.0 2 1.000 3
5 \*\*\* 3.000 0 0.0
6 \*\*\* 0.0 2 1.000
RED TOTAL PERCENTAGE OF LOST=0.837
BLUE TOTAL PERCENTAGE CF LOST=0.667

TIME= 310 SEC. AVERAGE RANGE BETWEEN RED AND BLUE=3423.4 M

UNIT LOCATION FORCE LEVEL STATUS LOST-PCT TARGETS

1 9 0.0 2 1.000

2 14 0.0 2 1.000

3 21 1.468 0 0.511

4 \*\*\* 0.0 2 1.000

5 \*\*\* 3.00C 0 0.0

6 \*\*\* 0.0 2 1.000

RED TOTAL PERCENTAGE OF LOST=0.837

BLUE TOTAL PERCENTAGE OF LOST=0.667

TI ME = 32 C SEC. AV ERAGE RANGE BETWEEN RED AND BLUE = 3383.7 M

TIME= 33 C SEC. AVERAGE PANGE BETWEEN RED AND BLUE= 3344.0 M

UNIT LOCATION FORCE LEVEL STATUS LOST-PCT TARGETS

1 9 0.0 2 1.000
2 14 0.0 2 1.000
3 23 1.468 0 0.511
4 \*\*\* 0.0 2 1.000
5 \*\*\* 3.000 0 0.0
6 \*\*\* 0.0 2 1.000
RED TOTAL PERCENTAGE OF LOST=0.837
BLUE TOTAL PERCENTAGE OF LOST=0.667

TIME= 340 SEC. AVERAGE RANGE BETWEEN RED AND BLUE=3304.3 M

UNIT LOCATION FORCE LEVEL STATUS LOST-PCT TARGETS

1 9 0.0 2 1.000
2 14 0.0 2 1.000
3 24 1.468 0 0.511
4 \*\*\* C.0 2 1.000
5 \*\*\* 3.000 0 0.0
6 \*\*\* 0.0 2 1.000
RED TOTAL PERCENTAGE OF LOST=0.837
ELUE TOTAL PERCENTAGE CF LOST=0.667

TIME 350 SEC. AVERAGE PANGE BETWEEN RED AND BLUE 3264.6 M

UNIT LOCATION FORCE LEVEL STATUS LOST-PCT TARGETS

1 9 0.0 2 1.000
2 14 0.0 2 1.000
3 25 1.468 0 0.511
4 \*\*\* 0.0 2 1.000
5 \*\*\* 0.0 2 1.000
6 \*\*\* 0.0 2 1.000
RED TOTAL PERCENTAGE OF LOST=0.837
ELUE TOTAL PERCENTAGE OF LOST=0.667

TI ME= 36C SEC. AV ERAGE RANGE BETWEEN RED AND BLUE = 3224.9 M

LNIT LOCATION FORCE LEVEL STATUS LOST-PCT TARGETS

1 9 0.0 2 1.000
2 14 0.0 2 1.000
3 26 1.46 0 0.511
4 \*\*\* 0.0 2 1.000
5 \*\*\* 3.000 0 0.0
6 \*\*\* 0.0 2 1.000
FED TOTAL PERCENTAGE OF LOST=0.837
BLUE TOTAL PERCENTAGE OF LOST=0.667

TIME= 37C SEC. AVERAGE RANGE BETWEEN RED AND BLUE=3185.2 M

UNIT LOCATION FORCE LEVEL STATUS LOST-PCT TARGETS

1 9 0.0 2 1.000

2 14 0.0 2 1.000

3 27 1.468 0 0.511

4 \*\*\* 0.0 2 1.000

5 \*\*\* 3.000 0 0.0

6 \*\*\* 0.0 2 1.000

RED TOTAL PERCENTAGE OF LOST=0.837
BLUE TOTAL PERCENTAGE OF LOST=0.667

TIME= 380 SEC. AVERAGE RANGE BETWEEN RED AND BLUE=3145.5 M

LNIT LOCATION FORCE LEVEL STATUS LCST-PCT TARGETS

1 9 0.0 2 1.000
2 14 0.0 2 1.000
3 28 1.468 0 0.511
4 \*\*\* 0.0 2 1.000
5 \*\*\* 0.0 2 1.000
6 \*\*\* 0.0 2 1.000
RED TOTAL PERCENTAGE OF LOST=0.837
BLUE TOTAL PERCENTAGE OF LOST=0.667

TIME= 390 SEC. AVERAGE RANGE BETWEEN RED AND BLUE=3105.9 M

UNIT LOCATION FORCE LEVEL STATUS LOST-PCT TARGETS

1 9 0.0 2 1.000

2 14 0.0 2 1.000

3 29 1.468 0 0.511

4 \*\*\* 0.0 2 1.000

5 \*\*\* 3.00C 0 0.0

RED TOTAL PERCENTAGE OF LOST=0.837
BLUE TOTAL PERCENTAGE OF LOST=0.667

TIME = 400 SEC. AVERAGE RANGE BETWEEN RED AND BLUE = 3066.2 M

TIME 410 SEC. AVERAGE RANGE BETWEEN RED AND BLUE = 3026.5 M

LOST-PCT 1.000 1.000 FORCE LEVEL UNIT LOCAT ION STATUS TARGETS 14 22020 C. 0 1.468 0.511 \*\* 1.000 \*\*\* 3. 00C 0.0 RED TOTAL PERCENTAGE OF LOST=0.837
BLUE TOTAL PERCENTAGE OF LOST=0.667 1.000

TI ME = 420 SEC. AVERAGE PANGE BETWEEN RED AND BLUE = 2986.9 M

LNIT LOCATION FORCE LEVEL STATUS LOST-FCT TARGETS

1 9 0.0 2 1.000
2 14 0.0 2 1.000
3 32 C.874 1 0.709 5
4 \*\*\* 0.0 2 1.000
5 \*\*\* 2.909 1 0.030 3
6 \*\*\* 0.0 2 1.000

RED TOTAL PERCENTAGE OF LOST=0.903
BLUE TOTAL PERCENTAGE OF LOST=0.677

TIME = 430 SEC. AVERAGE RANGE BETWEEN RED AND BLUE=2986.9 M

LNIT LOCATION FORCE LEVEL STATUS LOST-PCT TARGETS

1 9 0.0 2 1.000
2 14 0.0 2 1.000
3 32 0.297 1 0.901 5
4 \*\*\* 0.0 2 1.000
5 \*\*\* 0.0 2 1.000
5 \*\*\* 0.0 2 1.000
RED TOTAL PERCENTAGE OF LOST=0.680

TIME = 440 SEC. AVERAGE RANGE BETWEEN RED AND BLUE = 2986.9 M

UNIT LOCATION FORCE LEVEL STATUS LOST-PCT TARGETS

1 9 0.0 2 1.000

3 32 0.0 2 1.000

4 \*\*\* 0.0 2 1.000

5 \*\*\* 2.879 1 0.040 3

FED TOTAL PERCENTAGE OF LOST=1.000

BLUE TOTAL PERCENTAGE CF LOST=0.680

\*\*\* RED FORCE IS ELIMINATED. END OF BATTLE.

#### LIST OF REFERENCES

- 1. U.S. Army Materiel Systems Analysis Activity Report 169, The AMSAA War Game (AMSWAG) Computer Combat Simulation, by Joe H. Hawkins, July 1976.
- Taylor, James G., Lanchester-type Models of Warfare, unpublished draft of monograph.
- 3. United States Army Combined Arms Center TP 11-76, Sensitivity Analysis of BLDM Acquisition and Firepower Allocation, by H. Kent Pickett and F. Joseph AuBuchon, November, 1976.
- 4. Taylor, James G., An Introduction to the Modeling of Force-on-Force Attrition in Combat Operations, Military Applications section of Operations Research Society of America, Washington, D.C., 1979 (to appear)
- 5. Bonder, S. and Homig, J., An Analytic Model of Ground Combat: Design and Application, paper presented at the 1971 U.S. Army Operations Research Symposium, September 1171.
- 6. Hagewood, E. and Wallace W., "Simulation of Tactical Alternative Responses (STAR)," M.S. Thesis, Naval Postgraduate School, Decem-er 1978.
- 7. Taylor, James G., Attrition Modeling, paper presented at 3rd Systems Science Seminar, München, Germany, April 1978.

### INITIAL DISTRIBUTION LIST

		No.	Copies
1.	Defense Documentation Center Cameron Station Alexandria, Virginia 22314		2
2.	Library, Code 0142 Naval Postgraduate School Monterey, CA 93940		2
3.	Department Chairman, Code 55 Department of Operations Research Naval Postgraduate School Monterey, CA 93940		1
4.	Professor J.G. Taylor, Code 55TW Department of Operations Research Naval Postgraduate School Monterey, CA 93940		5
5.	LTC R.S. Miller, USA, Code 55Mu Department of Operations Research Naval Postgraduate School Monterey, CA 93940		2
6.	Major Josef Smoler, ISRAEL Hapardes Hanishon 14 Rishon-Le-Zion	1	LO
7.	Professor James G. Hartman, Code 55Hh Department of Operations Research Naval Postgraduate School Monterey, CA 93940		1
8.	Mr. H. K. Weiss P.O. Box 2668 Palos Verdes Peninsula Palos Verdes, CA 90274		1
9.	Mr. Lawrence J. Low Senior Scientific Advisor SRI International 333 Ravenswood Avenue Menlo Park, CA 94025		1
10.	Mr. Karl H. Eulenstein CINCPAC Staff Box 13, J77 Camp Smith, HI 96861		1